

CS120 - Computer Science I

Lab #4

Fall 2014

Due: At the end of lab.

The purpose of this lab is to use loops to calculate approximations of some standard mathematical values. Irrational numbers, such as π and e , can only be approximated using mathematical formula. In this lab we'll write two different programs to calculate two approximations.

1 π

Begin by creating a new program called `piLab4SectionX.cpp` (where X is your section number). As always include your name, date, etc. in a comment block at the beginning.

Values like π can be approximated using an infinite sum. Each term in the sum moves the total a little closer to the goal value. One of the simpler formulas to approximate π is:

$$\pi = 4 \sum_{k=1}^{\infty} \frac{-1^{(k+1)}}{2k-1} \quad (1)$$

(Other formula can be found at: <http://mathworld.wolfram.com/Pi.html>.) Using this formula requires a loop that increase k from 1 to some upper bound. At each step of the loop the next term in the sum is added to a running total. Your output should show both the value of k and the current approximation. For example, the first 4 approximations are:

```
k  $\pi$ 
1 4
2 2.666
3 3.466
4 2.895
```

To test your program use a large upper bound and check that the total is approaching π .

When you are done with the program submit it using `cscheckin`.

2 e

Create another new program called `eLab4SectionX.cpp` (where X is your section number). As always include your name, date, etc. in a comment block at the beginning.

One of the simpler formulas to approximate e is:

$$e = \sum_{k=0}^{\infty} \frac{1}{k!} \quad (2)$$

(Other formula can be found at: <http://mathworld.wolfram.com/e.html>.) As with π using this formula requires a loop that increase k from 0 to some upper bound (note that the starting bound is now 0). At each step of the loop the next term in the sum is added to a running total. However, the sum includes the *factorial* of k , which is defined as:

$$k! = 1 * 2 * 3 * \dots * k \quad (3)$$

with

$$0! = 1 \quad (4)$$

In order to calculate the factorial you will need to use an *nested* loop that counts from 1 to k .

Your output should show both the value of k and the current approximation. For example, the first 4 approximations are:

```
k e
1 1
2 2
3 2.5
4 2.666
```

To test your program use a large upper bound and check that the total is approaching e . However, the factorial grow large very quickly, so if your upper bound is too large you will get an overflow error (the value of $k!$ will be too large to be stored).

When you are done with the program submit it using cscheckin.