#### Signed Messages

- Traitors ability to lie makes Byzantine General Problem so difficult.
- If we restrict this ability, then the problem becomes easier
- Use authentication, i.e. allow generals to send unforgeable signed messages.

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#### Signed Messages

Assumptions about Signed Messages

A1: every message that is sent is delivered correctly

A2: the receiver of a message knows who send it

A3: the absence of a message can be detected

A4: a loyal general's signature cannot be forged, and any alteration of the contents of his signed messages can be detected. Anyone can verify the authenticity of a general's signature

Note: no assumptions are made about a traitor general, i.e. a traitor can forge the signature of another traitor.

#### Signed Messages

- Signed message algorithm assumes a choice function
  - if a set V has one single element v, then choice(V) = v
  - choice( $\Phi$ ) = R, where  $\Phi$  is the empty set
    - » RETREAT is default
  - choice(A,R) = R
    - » RETREAT is default
  - set V is <u>not</u> a multiset (recall definition of a multiset)
  - thus set V can have at most 2 elements, e.g.  $V = \{A,R\}$ .

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# Signed Messages

- Signing notation
  - let v:i be the value v signed by general i
  - let v:i:j be the message v:i counter-signed by general j
- ullet each general *i* maintains his own set  $V_i$  containing all orders he received
- Note: do not confuse the set  $V_i$  of orders the general received with the set of all messages he received. Many different messages may have the same order.

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#### BGP: Signed Message Solution

SM(m) -- from Lam82

Initially  $V_i = \Phi$ 

- 1) The commander signs and sends his value to every lieutenant
- 2) For each i
  - A) If lieutenant *i* receives a message of the form v:0 from the commander and he has not yet received any order, then
    - i) he lets  $V_i$  equal  $\{v\}$
    - ii) he sends the message v:0:i to every other lieutenant
  - B) If lieutenant *i* receives a message of the form  $v:0:j_1:...:j_k$  and v is not in the set  $V_i$ , then
    - i) he adds v to  $V_i$
    - ii) if k < m, then he sends the message  $v: 0: j_1: ...: j_k: i$  to every lieutenant other than  $j_1, ..., j_k$

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#### Algorithm SM(m)

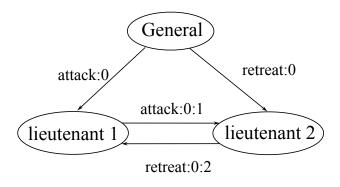
• the SM(m) algorithm for signed messages works for

$$N \ge m + 2$$

i.e. want non faulty commander and at least one non faulty lieutenant

- How does one know when one does not receive any more messages?
  - by *missing message assumption* A3, we can tell when all messages have been received
  - this can be implemented by using synchronized rounds
- Now traitor can be detected!
  - e.g. 2 correctly signed values => general is traitor

• example, general is traitor



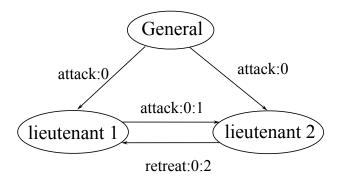
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# Algorithm SM(m)

• example, lieutenant 2 is traitor



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- example:
  - -SM(0)
    - » general sends v:0 to all lieutenants
    - » processor *i* receives v:0  $V_i = \{v\}$
  - SM(1)
    - » each lieut. countersigns and rebroadcasts  $v:\theta$
    - » processor *i* receives (*v*:0:1, *v*:0:2,..., *v*:0:(*N*-1))

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# Algorithm SM(m)

- case 1: commander loyal, lieutenant j = traitor
  - » all values <u>except</u> v:0:j are v

 $\Rightarrow v \in V_i \quad \forall \text{ loyal lieut. i}$ 

» processor *j* cannot tamper

 $\Rightarrow V_i = \{v\} \quad \forall \text{ loyal lieut. i}$ 

- case 2: commander = traitor, => all lieut. loyal
  - » all lieutenants correctly forward what they received
    - agreement: yes
    - validity: N/A

- e.g.:
  - SM(2)
    - » each lieut. countersigns and rebroadcasts all messages from the previous round
    - » processor i has/receives
      - *v:0*
      - *v*:0:1, *v*:0:2, ... , *v*:0:(*N*-1)

- original message
- <u>v:0:1:1,</u> v:0:1:2, v:0:1:3, ..., v:0:1:N-1 v:0:2:1, <u>v:0:2:2,</u> v:0:2:3, ..., v:0:2:N-1

after 1st rebroadcast

v:0:N-1:1, v:0:N-1:2, v:0:N-1:3, ..., <u>v:0:N-1:N-1</u>

after 2nd rebroadcast

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### Algorithm SM(m)

- case 1: commander loyal, 2 lieutenants are traitors
  - » want each loyal lieut to get  $V = \{v\}$
  - » round  $0 \Rightarrow$  all loyal lieuts get v from commander
  - » other rounds:
    - traitor cannot tamper
    - => all messages are v or  $\Phi$
- case 2: commander traitor + 1 lieut. traitor
  - » round 0: all loyal lieuts receive v:0
  - » round 1:
    - traitors send one value or  $\Phi$
  - » round 2:
    - another exchange (in case traitor caused split in last round)
    - traitor still can <u>not</u> introduce new value
      - => agreement: yes validity: N/A

#### Cost of signed message

- encoding one bit in a code-word so faulty processor cannot "stumble" on it.
- e.g.
  - » unreliability of the system  $F_S = 10^{-10}/h$
  - » unreliability of single processor  $F_p = 10^{-4}/h$
  - » want: Probability of randomly generated valid code word

$$P = \frac{10^{-10}}{10^{-4}} = 10^{-6} \approx 2^{-20}$$

- » given 2<sup>i</sup> valid codewords, want (20+i) bits/signature
- » e.g. Attack/Retrieve
  - $=> 2^{1}$
  - => 21 bit signature

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#### Agreement

#### Important notes:

- there is no way to guarantee that different processors will get the same value from a possibly faulty input device, except having the processors communicate among themselves to solve the Byz.Gen. Problem.
- faulty input device may provide meaningless input values
  - » all that Byz.Gen. solution can do is guarantee that all processors use the same input value.
  - » if input is important, then use redundant input devices
  - » redundant inputs cannot achieve reliability. It is still necessary to insure that all non-faulty processors use the redundant data to produce the same output.

#### Agreement

- Implementing BGP is no problem
- The problem is implementing a message passing system that yields respective assumptions, i.e.:

A1: every message that is sent is delivered correctly

A2: the receiver of a message knows who send it

A3: the absence of a message can be detected

A4: a loyal general's signature cannot be forged, and any alteration of the contents of his signed messages can be detected. Anyone can verify the authenticity of a general's signature

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