

Chapter 3: Data Transmission

Terminology (1)

- Transmitter
- Receiver
- Medium
 - Guided medium
 - e.g. twisted pair, optical fiber
 - Unguided medium
 - e.g. air, water, vacuum

Terminology (2)

- Direct link
 - No intermediate devices
- Point-to-point
 - Direct link
 - Only 2 devices share link
- Multi-point
 - More than two devices share the link

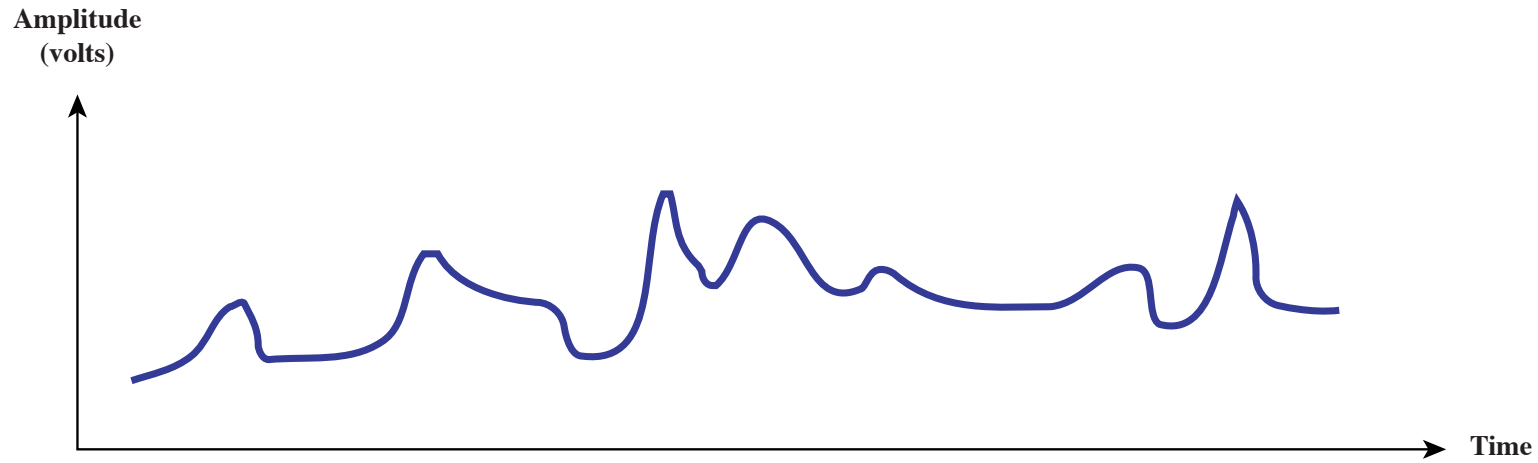
Terminology (3)

- Simplex
 - One direction
 - e.g. Television
- Half duplex
 - Either direction, but only one way at a time
 - e.g. police radio
- Full duplex
 - Both directions at the same time
 - e.g. telephone

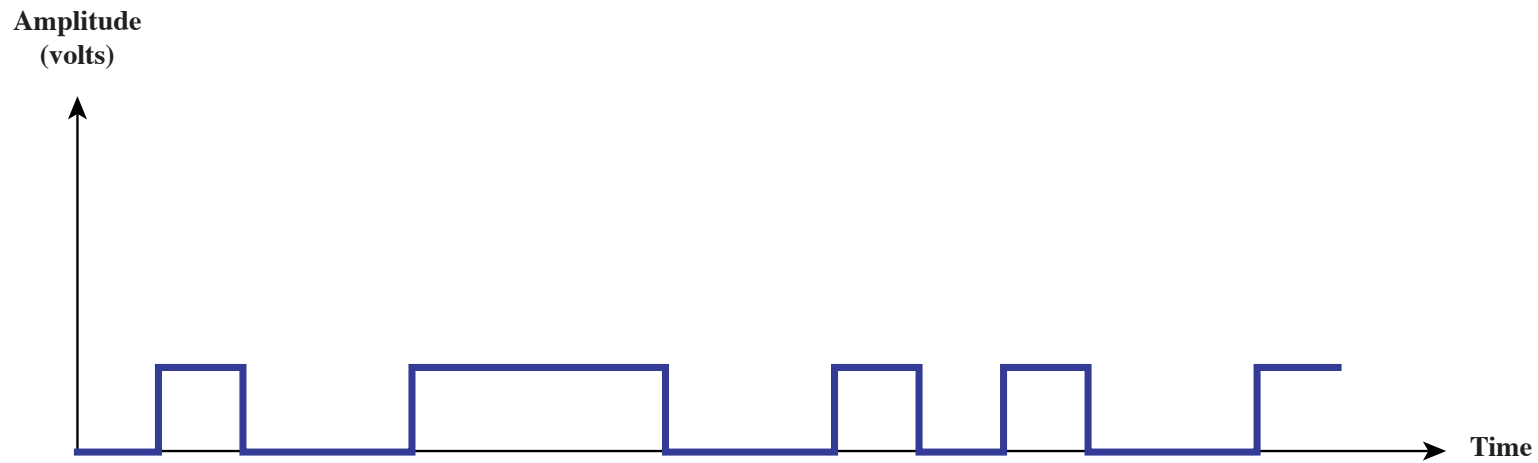
Frequency, Spectrum and Bandwidth

- Time domain concepts
 - Analog signal
 - Varies in a smooth way over time
 - Digital signal
 - Maintains a constant level then changes to another constant level
 - Periodic signal
 - Pattern repeated over time
 - Aperiodic signal
 - Pattern not repeated over time

Analogue & Digital Signals

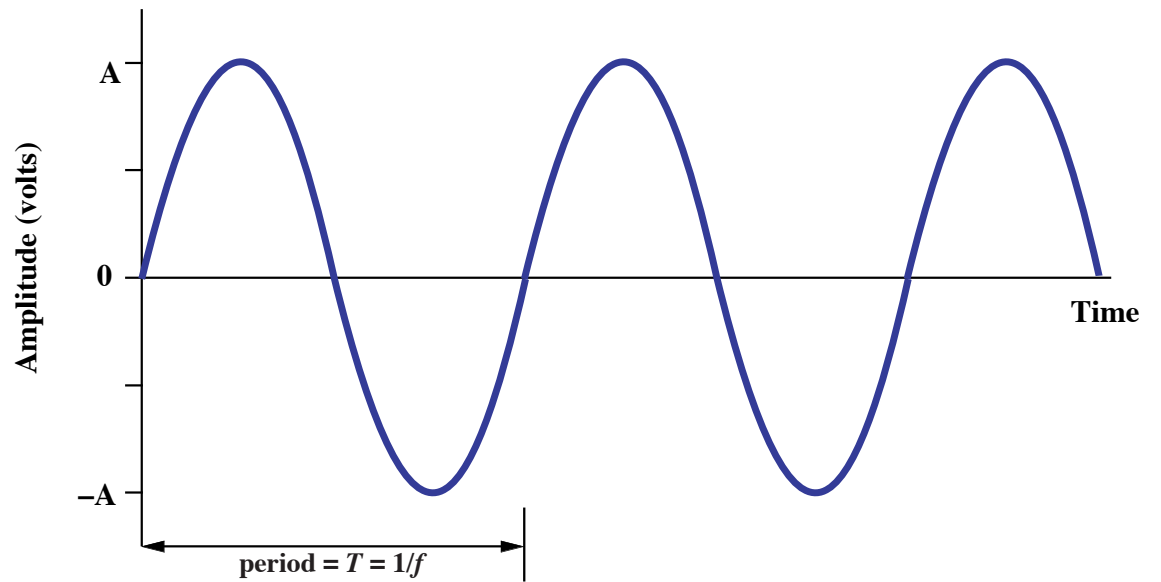


(a) Analog

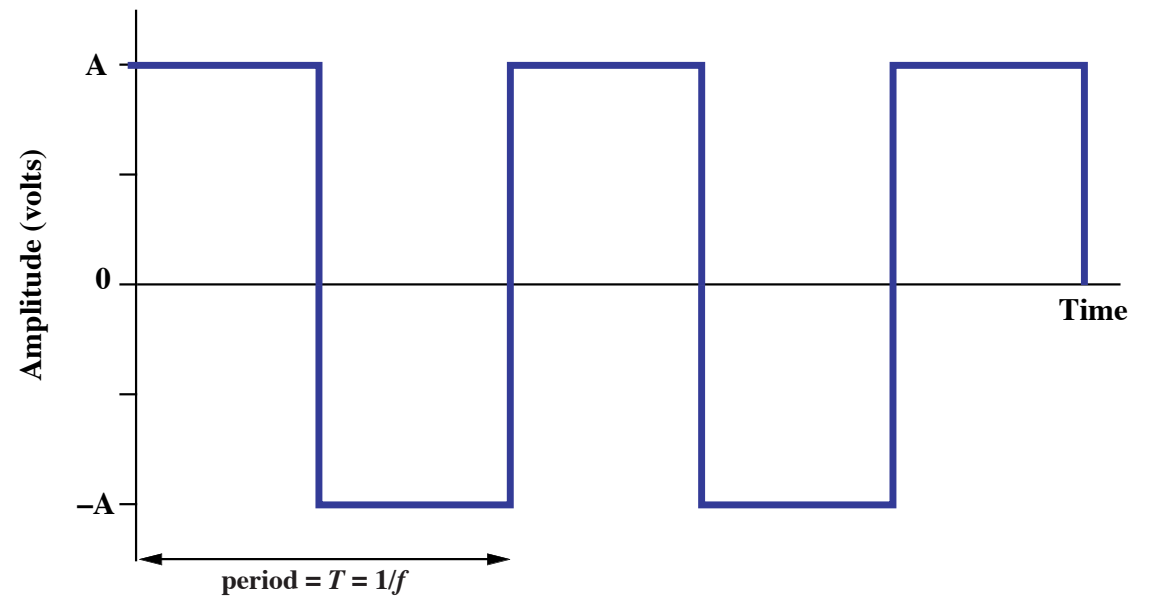


(b) Digital

Periodic Signals



(a) Sine wave



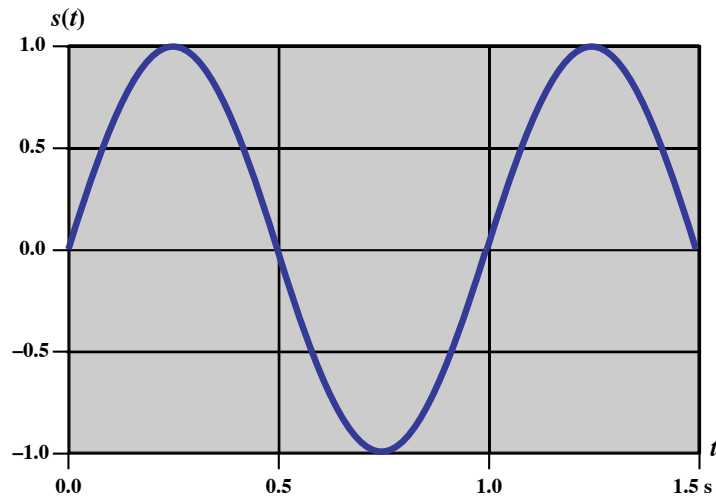
(b) Square wave

Sine Wave

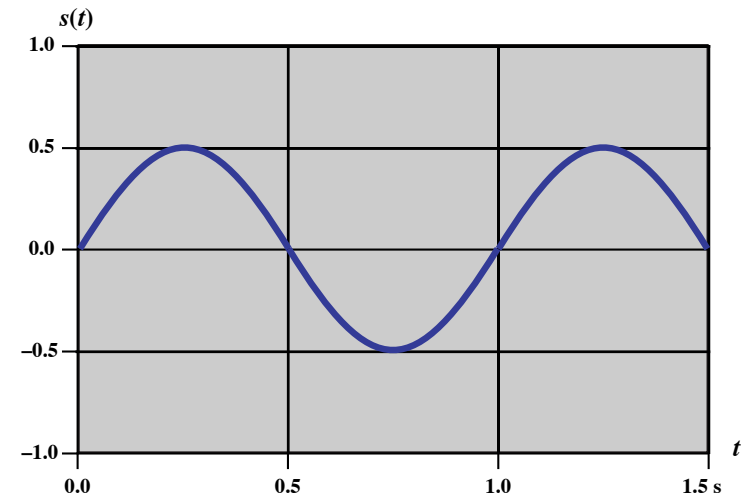
- Peak Amplitude (A)
 - maximum strength of signal, in volts
- Frequency (f)
 - Rate of change of signal, in Hertz (Hz) or cycles per second
 - Period = time for one repetition (T), $T = 1/f$
- Phase (ϕ)
 - Relative position in time
- Periodic signal $s(t + T) = s(t)$
- General wave $s(t) = A \sin(2\pi ft + \Phi)$

Periodic Signal: e.g. Sine Waves

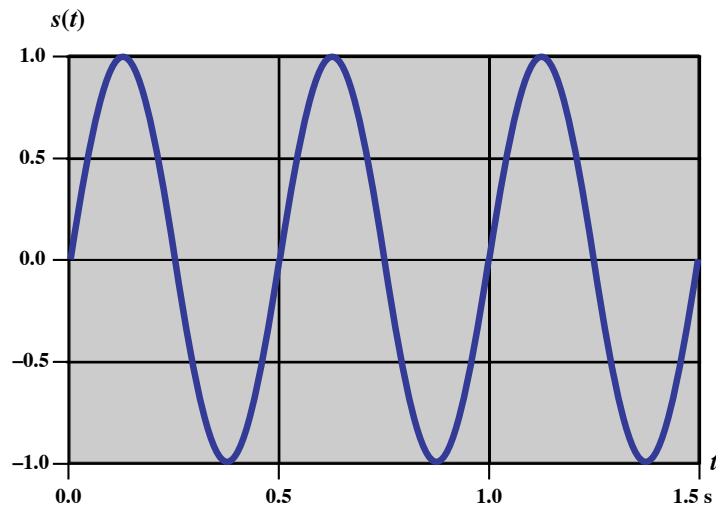
$$s(t) = A \sin(2\pi ft + \Phi)$$



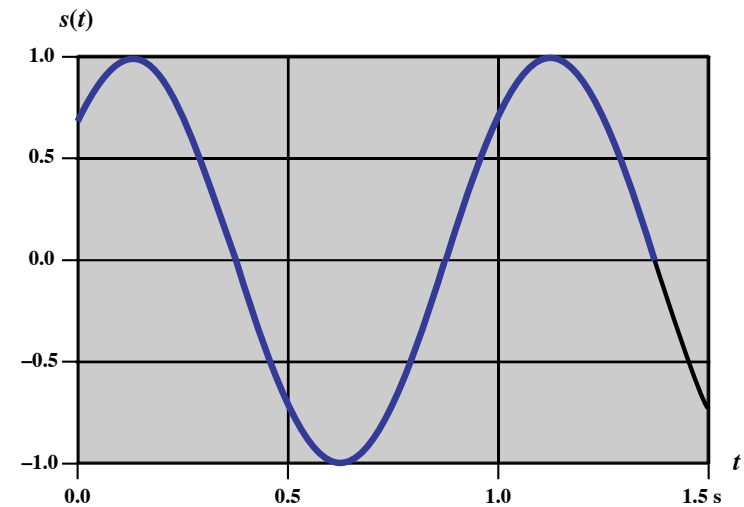
(a) $A = 1, f = 1, \phi = 0$



(b) $A = 0.5, f = 1, \phi = 0$



(c) $A = 1, f = 2, \phi = 0$



(d) $A = 1, f = 1, \phi = \pi/4$

Wavelength

- Distance occupied by one cycle
- Distance between two points of corresponding phase in two consecutive cycles
- Wavelength λ
- Assuming signal velocity v

$$\lambda = vT \quad [\text{unit is m}]$$

$$\lambda f = v$$

$$c = 3 \cdot 10^8 \text{ m/s (speed of light in free space)}$$

Frequency Domain Concepts

- Signal is usually made up of many frequencies
- Components are sine waves
- It can be shown (Fourier analysis) that any signal is made up of component sine waves
- One can plot frequency domain functions

Building block for waves

- What is a square wave?
 - What frequency components are digital signals composed of?
 - How many components do I need to recreate a square wave?
 - What is a realistic spectrum?
 - Where is the main energy of the signal?
 - Below is a representation of a square wave with amplitude A:

$$s(t) = \frac{A}{\pi} \sum_{k \text{ odd}, k=1}^{\infty} \frac{1}{k} \sin(2\pi kft)$$

Physical Aspects

- Limited Bandwidth
 - Fourier Analysis

$$v(t) = a_0 + \sum_{n=1}^{\infty} a_n \cos n\omega_0 t + \sum_{n=1}^{\infty} b_n \sin n\omega_0 t$$

$$a_0 = \frac{1}{T} \int_0^T v(t) dt$$

$$a_n = \frac{2}{T} \int_0^T v(t) \cos(n\omega_0 t) dt$$

$$b_n = \frac{2}{T} \int_0^T v(t) \sin(n\omega_0 t) dt$$

$v(t)$ = voltage as a function of time

ω_0 = fundamental frequency component in radians / second

f_0 = fundamental frequency in Hz

$T = 1/f_0$ = period in seconds

Physical Aspects

- Limited Bandwidth (cont.)

- Unipolar

$$v(t) = \frac{V}{2} + \frac{2V}{\pi} \left\{ \cos \omega_0 t - \frac{1}{3} \cos 3\omega_0 t + \frac{1}{5} \cos 5\omega_0 t - \dots \right\}$$

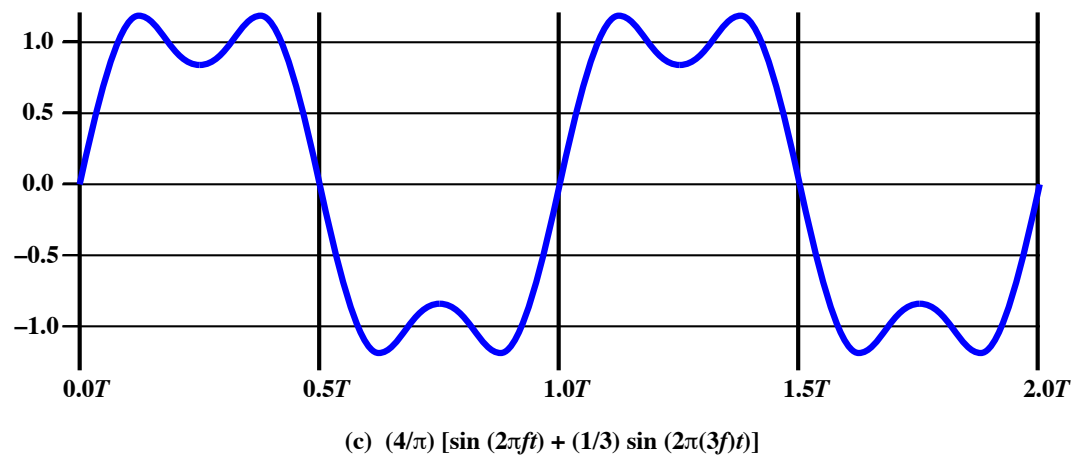
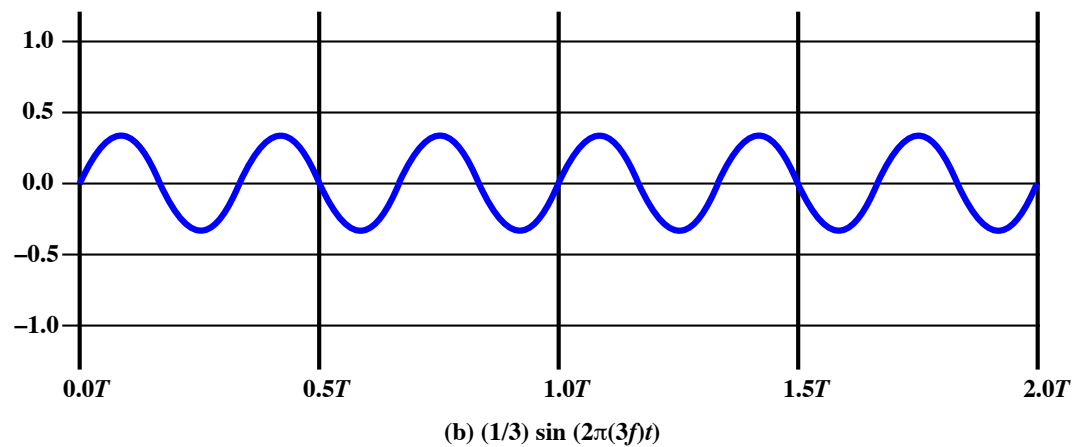
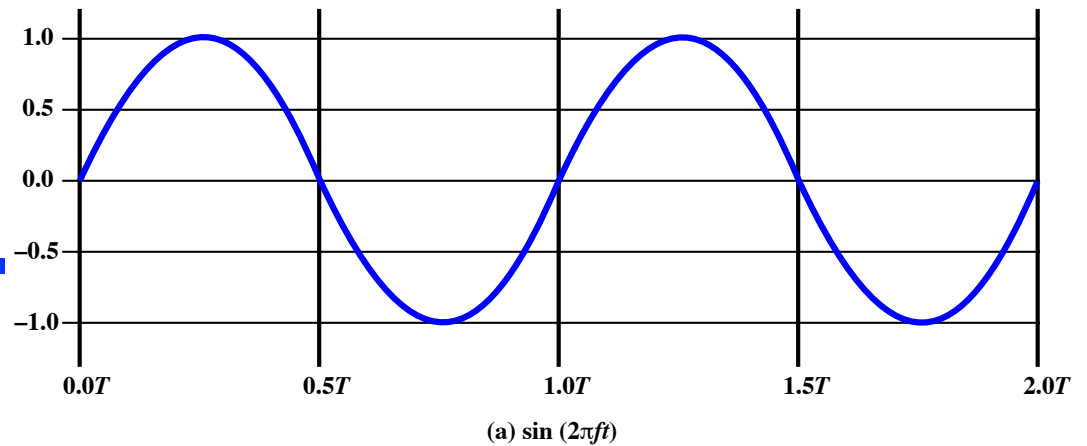
- Bipolar

$$v(t) = \frac{4V}{\pi} \left\{ \cos \omega_0 t - \frac{1}{3} \cos 3\omega_0 t + \frac{1}{5} \cos 5\omega_0 t - \dots \right\}$$

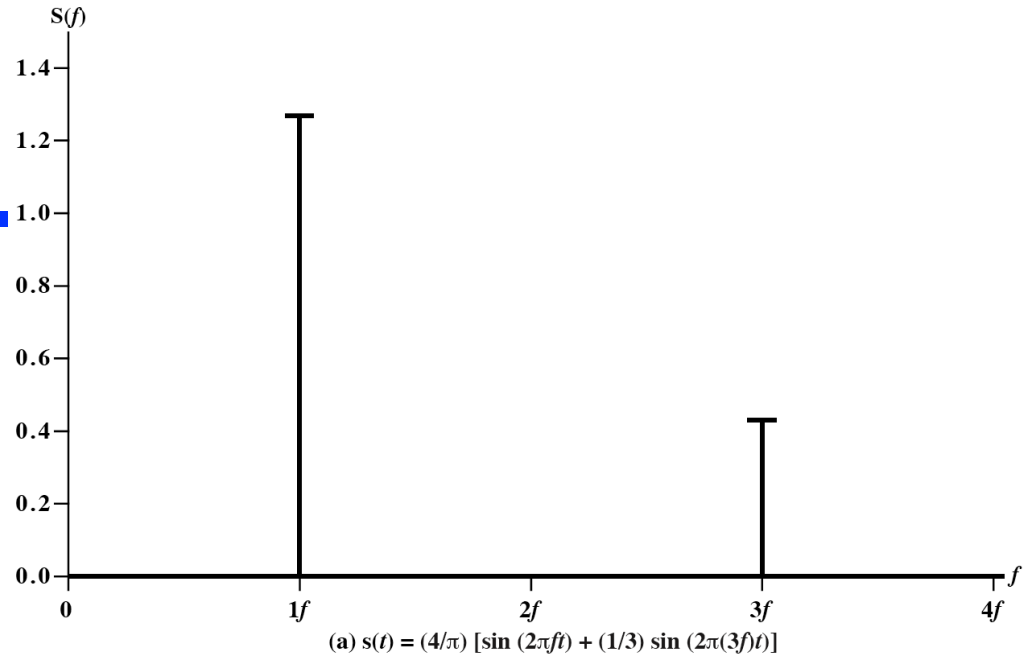
How much bandwidth do we need?

What are the trade-offs if we compromise bandwidth?

Addition of Frequency Components ($T=1/f$)

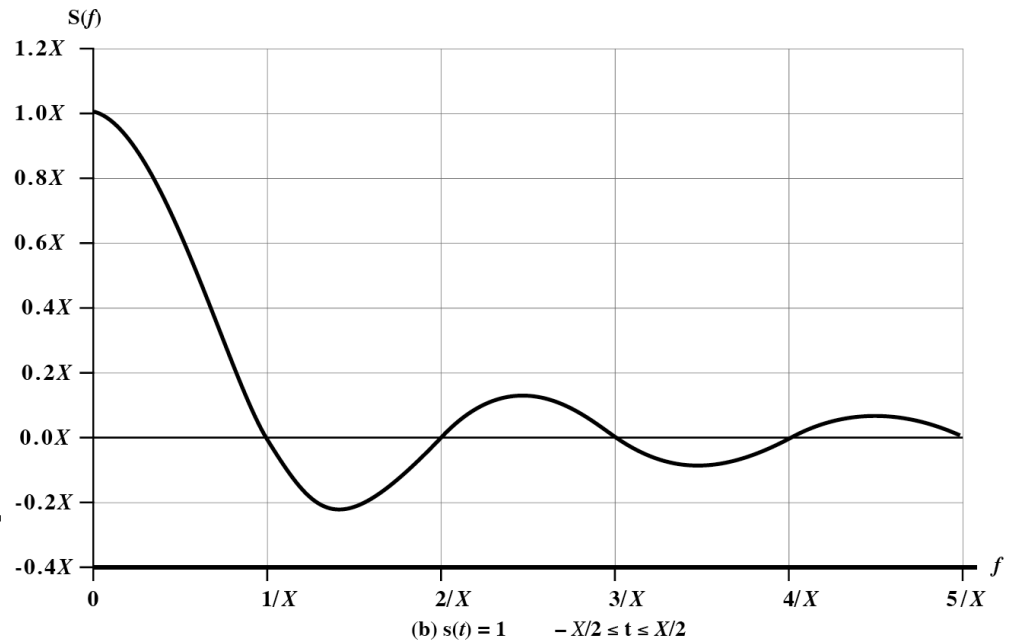


Spectrum of previous example



Single pulse:

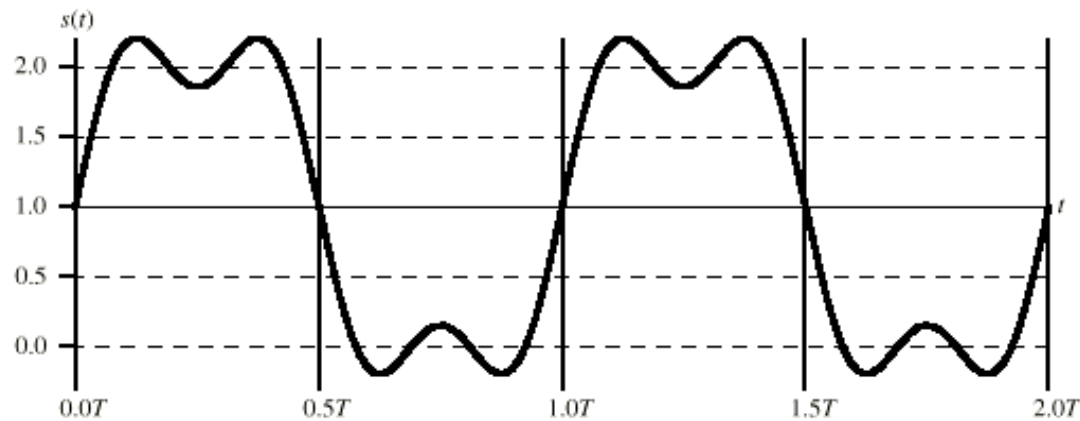
between $-X/2$ and $X/2$



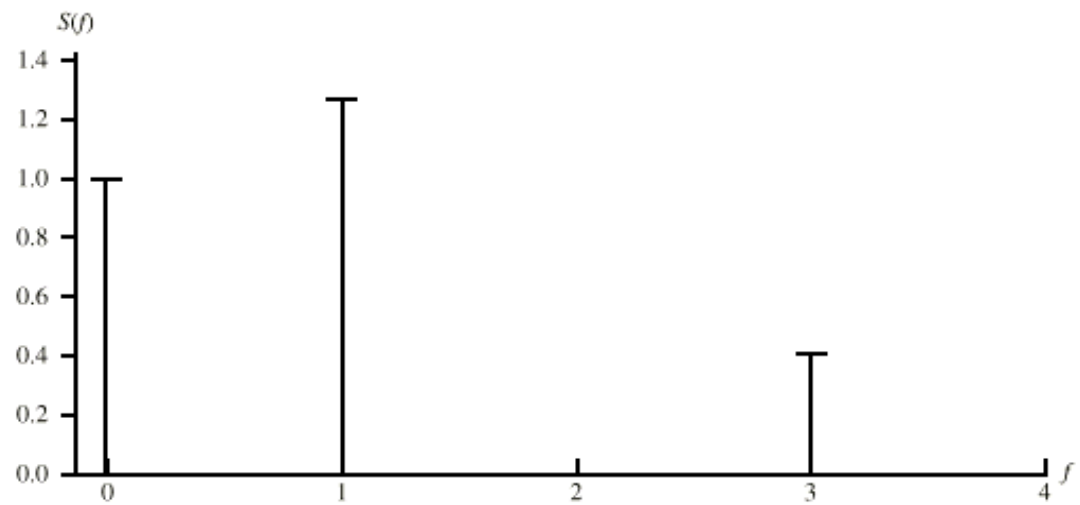
Spectrum & Bandwidth

- Spectrum
 - range of frequencies contained in signal
- Absolute bandwidth
 - width of spectrum
- Effective bandwidth
 - Often just *bandwidth*
 - Narrow band of frequencies containing most of the energy
- DC Component
 - Component of zero frequency

Signal with DC Component



(a) $s(t) = 1 + (4/10) [\sin(2\pi ft) + (1/3) \sin(2\pi (3f)t)]$



(b) $S(f)$

Data Rate and Bandwidth

- Any transmission system has a limited band of frequencies
- This limits the data rate that can be carried
- Issues
 - The more bandwidth the less distortion
 - Where is the bulk of the energy?

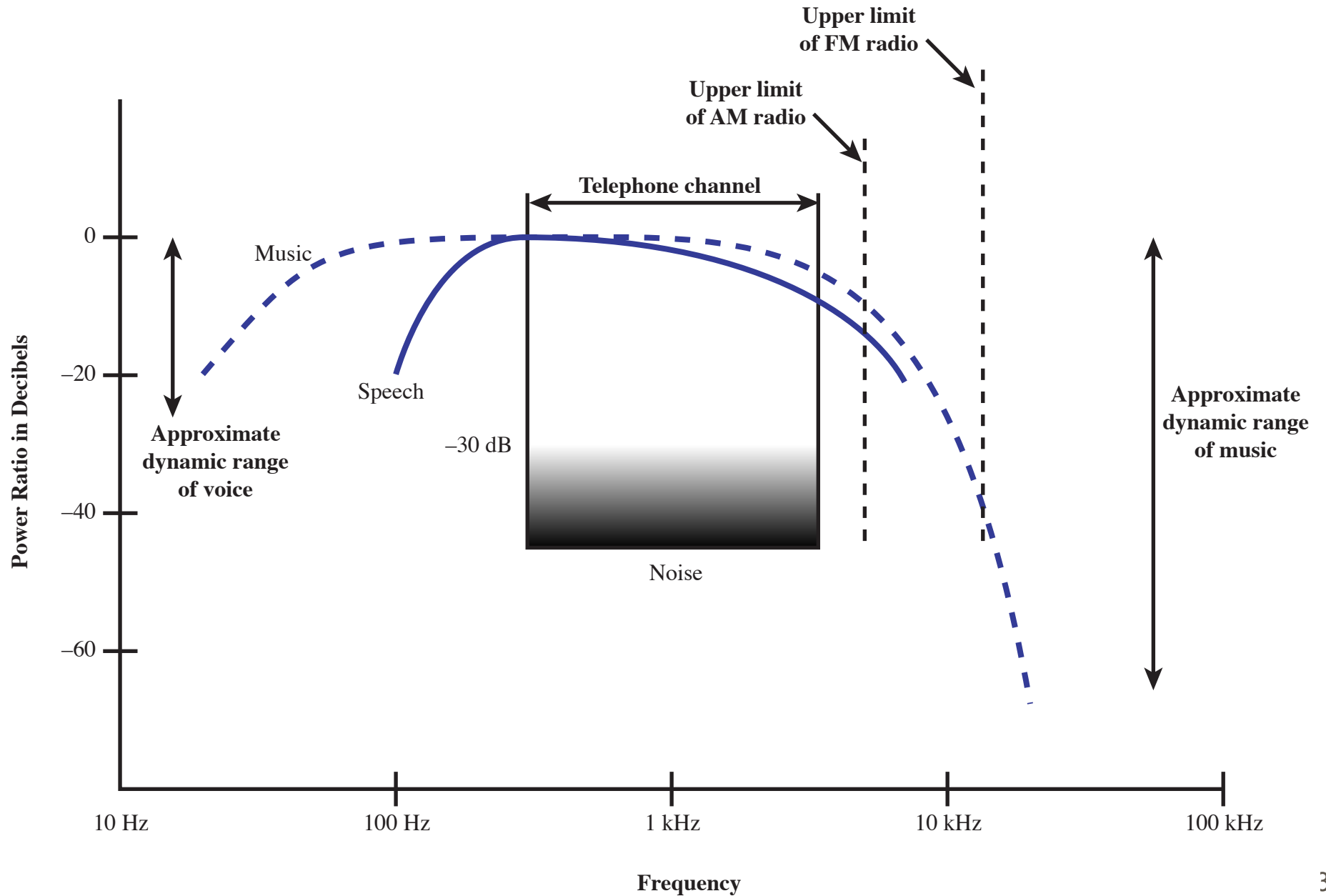
Analog and Digital Data Transmission

- Data
 - Entities that convey meaning
- Signals
 - Electric or electromagnetic representations of data
- Transmission
 - Communication of data by propagation and processing of signals

Analog and Digital Data

- Analog
 - Continuous values within some interval
 - e.g. sound, video
- Digital
 - Discrete values
 - e.g. text, integers

Acoustic Spectrum (Analog)



Analog and Digital Signals

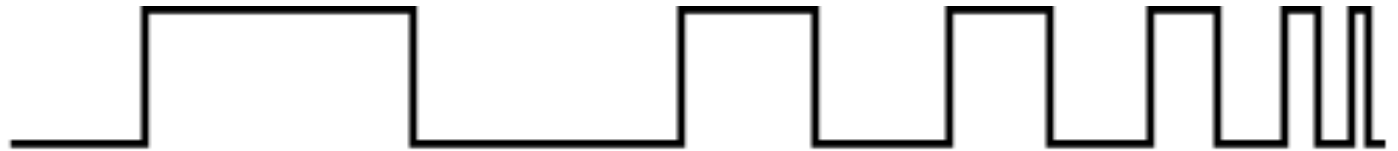
- Means by which data are propagated
- Analog
 - Continuously variable
 - Various media
 - wire, fiber optic, space
 - Speech bandwidth 100Hz to 7kHz
 - Telephone bandwidth 300Hz to 3400Hz
 - Video bandwidth 4MHz
- Digital
 - Use two DC components

Advantages & Disadvantages of Digital

- Cheaper
- Less susceptible to noise
- Greater attenuation
 - Pulses become rounded and smaller
 - Leads to loss of information

Attenuation of Digital Signals

Voltage at
transmitting end



Voltage at
receiving end

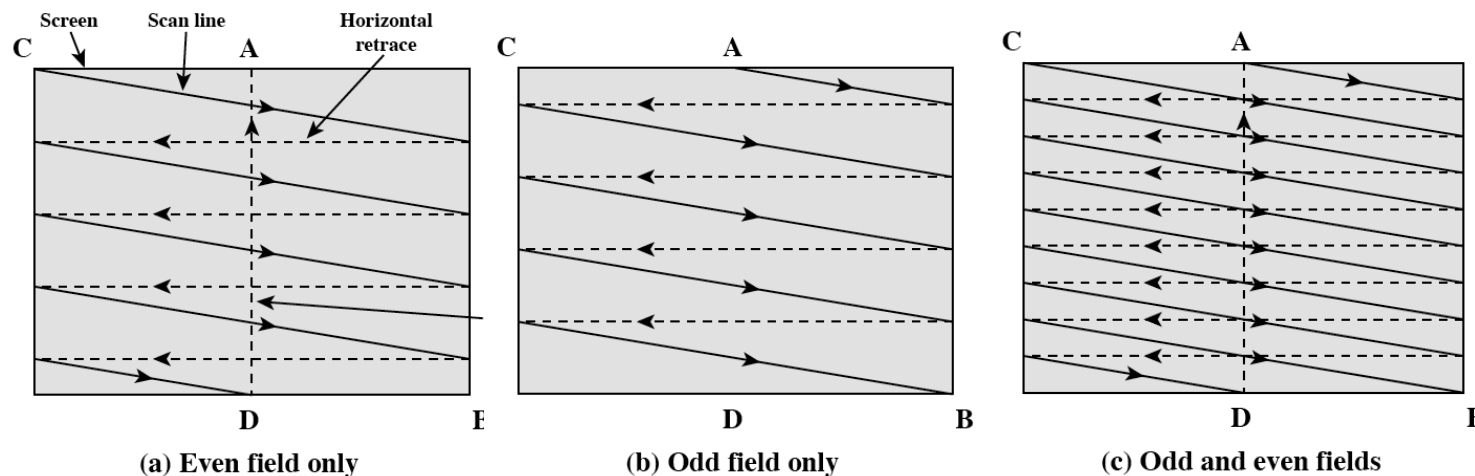


Components of Speech

- Frequency range (of hearing) 20Hz-20kHz
 - Speech 100Hz-7kHz
- Easily converted into electromagnetic signal for transmission
- Sound frequencies with varying volume converted into electromagnetic frequencies with varying voltage
- Limit frequency range for voice channel
 - 300-3400Hz

Video Components

- USA - 483 lines scanned per frame at 30 frames per second
 - 525 lines but 42 lost during vertical retrace
- So 525 lines x 30 scans = 15750 lines per second
 - $63.5\mu\text{s}$ per line, ($11\mu\text{s}$ for retrace, so $52.5\mu\text{s}$ per video line)
- Max frequency if line alternates black and white
- Horizontal resolution is about 450 lines giving 225 cycles of wave in $52.5\mu\text{s}$
- Max frequency of 4.2MHz

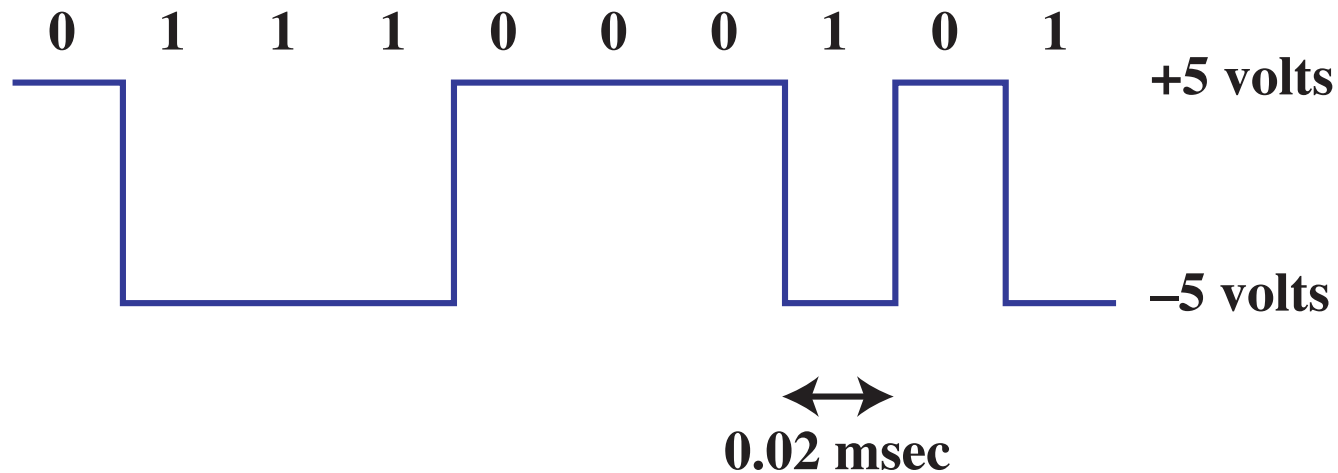


Binary Digital Data

- From computer terminals etc.
- Two dc components
- Bandwidth depends on data rate

Conversion of PC Input to Digital Signal

- as generated by computers etc.
- has two dc components
- bandwidth depends on data rate

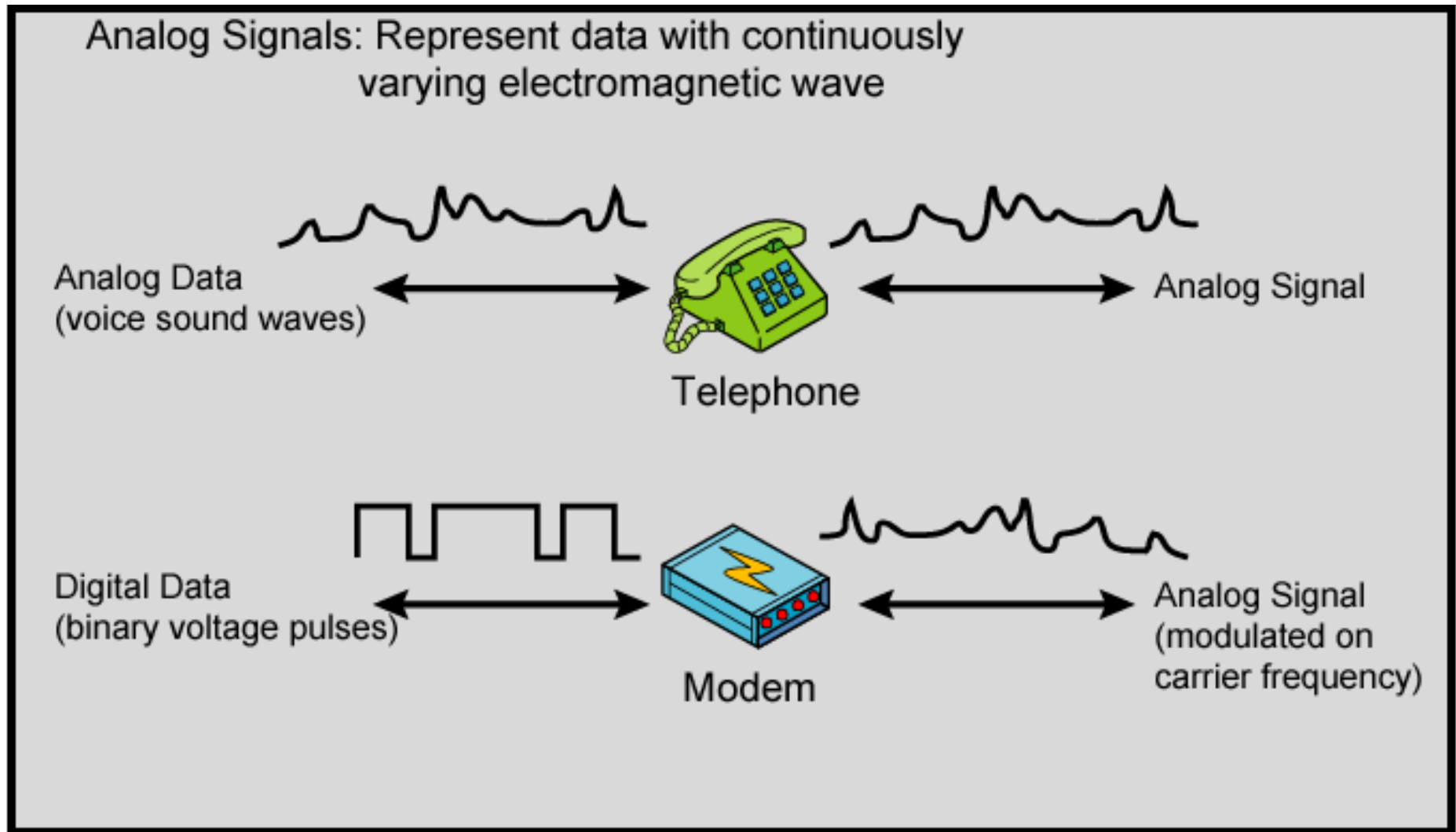


User input at a PC is converted into a stream of binary digits (1s and 0s). In this graph of a typical digital signal, binary one is represented by -5 volts and binary zero is represented by $+5$ volts. The signal for each bit has a duration of 0.02 msec, giving a data rate of $50,000$ bits per second (50 kbps).

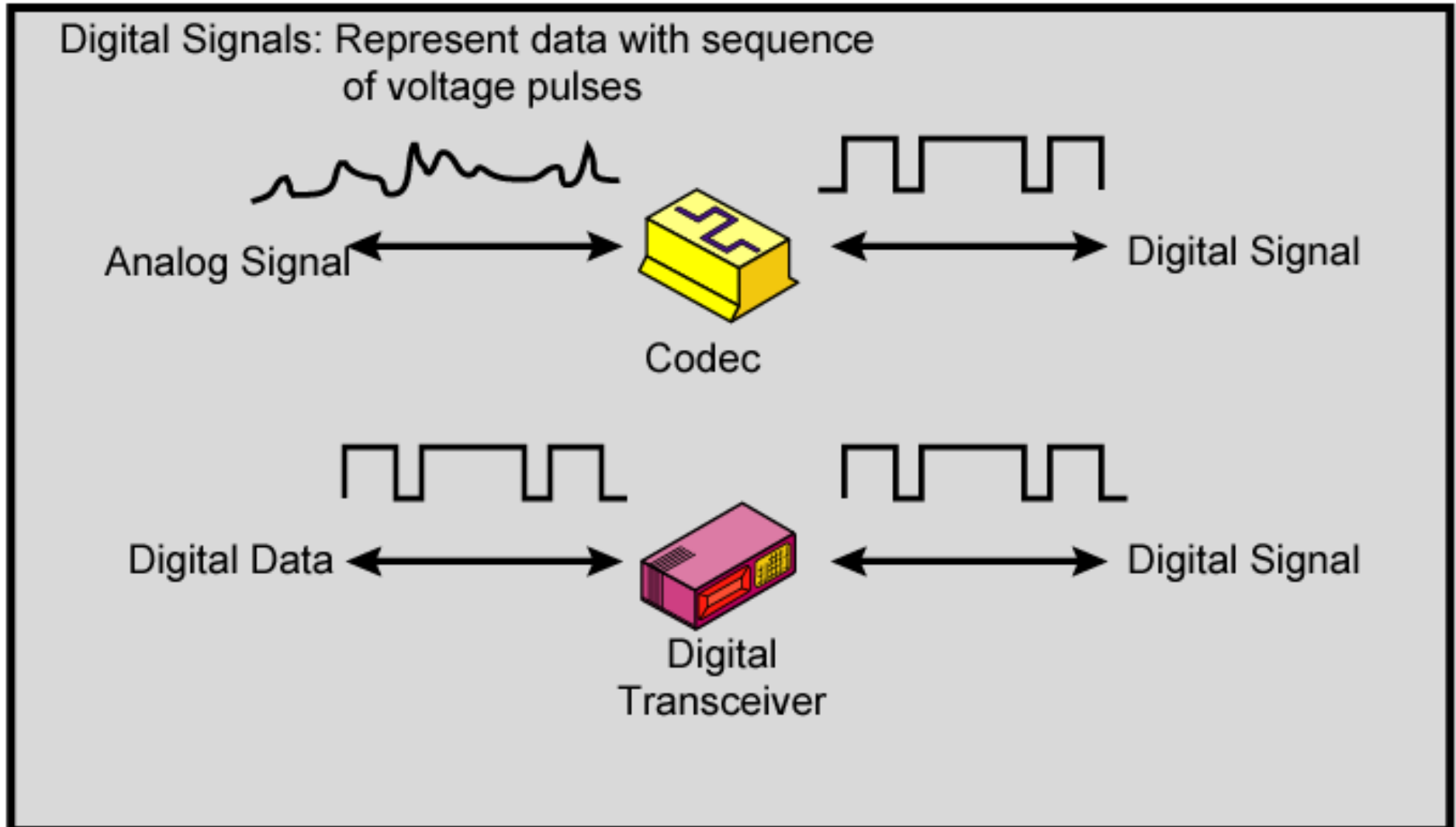
Data and Signals

- Usually use digital signals for digital data and analog signals for analog data
- Can use analog signal to carry digital data
 - Modem
- Can use digital signal to carry analog data
 - Compact Disc audio

Analog Signals Carrying Analog and Digital Data



Digital Signals Carrying Analog and Digital Data



Transmission Impairments

- Signal received may differ from signal transmitted causing:
 - analog - degradation of signal quality
 - digital - bit errors
- Most significant impairments are
 - attenuation and attenuation distortion
 - delay distortion
 - noise

Attenuation

- Signal strength falls off with distance
- Depends on medium
- Received signal strength:
 - must be enough to be detected
 - must be sufficiently higher than noise to be received without error
- Attenuation is an increasing function of frequency

Delay Distortion

- Only in guided media
- Propagation velocity varies with frequency

Noise (1)

- Additional signals inserted between transmitter and receiver
- Thermal
 - Due to thermal agitation of electrons
 - Uniformly distributed
 - White noise
- Intermodulation
 - Signals that are the sum and difference of original frequencies sharing a medium

Noise (2)

- Crosstalk
 - A signal from one line is picked up by another
- Impulse
 - Irregular pulses or spikes
 - e.g. External electromagnetic interference
 - Short duration
 - High amplitude

Digital Transmission

- Concerned with content
- Integrity endangered by noise, attenuation etc.
- Repeaters
 - Repeater receives signal
 - Extracts bit pattern
 - Retransmits
 - Attenuation is overcome
 - Noise is not amplified

Analog Transmission

- Analog signal transmitted without regard to content
- May be analog or digital data
- Attenuated over distance
- Use amplifiers to boost signal
- Also amplifies noise

Advantages of Digital Transmission

- Digital technology
 - Low cost LSI/VLSI technology
- Data integrity
 - Longer distances over lower quality lines
- Capacity utilization
 - High bandwidth links economical
 - High degree of multiplexing easier with digital techniques
- Security & Privacy
 - Encryption
- Integration
 - Can treat analog and digital data similarly

Channel Capacity

- Data rate
 - In bits per second, bps (not Bps)
 - Rate at which data can be communicated
- Bandwidth
 - In cycles per second of Hertz, Hz
 - Constrained by transmitter and medium
- Convention: not all k' s are equal
 - data rates are given as power of 10
 - e.g., kHz is 1000Hz
 - data is given in terms of power of 2
 - e.g., KByte is 1024 Bytes

Nyquist Bandwidth

- If rate of signal transmission is $2B$ then a signal with frequencies no greater than B is sufficient to carry the signal rate.
 - Why? Assume we have a square wave of repeating 101010. If a positive pulse is a 1 and a negative pulse is 0, then each pulse lasts $1/2 T_1$ ($T_1 = 1/f_1$) and the data rate is $2f_1$ bits per second.

Nyquist Bandwidth

- If we limit the components to a maximum frequency (restrict the bandwidth) we need to make sure the signal is accurately represented.
- Based on the accuracy we require, the bandwidth can carry a particular data rate. The theoretical maximum communication limit is given by the **Nyquist** formula:

$$C = 2B \log_2 M$$

C = capacity or data transfer rate in bps

B = bandwidth (in hertz)

M = number of possible signaling levels

Signal Strength

- An important parameter in communication is the strength of the signal transmitted. Even more important is the strength being received.
- As signal propagates it will be *attenuated* (decreased)
- Amplifiers* are inserted to increase signal strength
- Gains, losses and relative levels of signals are expressed in decibels
 - This is a logarithmic scale, but strength usually falls logarithmically
 - Calculation of gains and losses involves simple addition and subtraction
- Decibel measure of difference in two power levels is

$$N_{dB} = 10 \log_{10} \frac{P_1}{P_2}$$

Physical Aspects

- Signal Attenuation and Distortion
 - As a signal propagates across a transmission medium its amplitude decreases. This is known as **signal attenuation**.
 - A typical signal consists of a composition of many frequency components (Fourier Analysis). Due to the limited transmission bandwidth of a medium, the higher frequency components may not be able to be transmitted.
 - Recall the **Nyquist** formula

$$C = 2B \log_2 M$$

$$\log_2(x) = \frac{\ln(x)}{\ln(2)}$$

Delay Distortion

- Different frequency components of a signal
 - are attenuated differently, and
 - travel at different speeds through guided media

- This may lead to **delay distortion**

Shannon capacity

- A transmission line may experience interference from a number of sources, called **noise**. Noise is measured in terms of signal to noise power ratio, expressed in decibels:

$$\left(\frac{S}{N}\right)_{dB} = 10 \log_{10} \left(\frac{S}{N}\right) \text{dB}$$

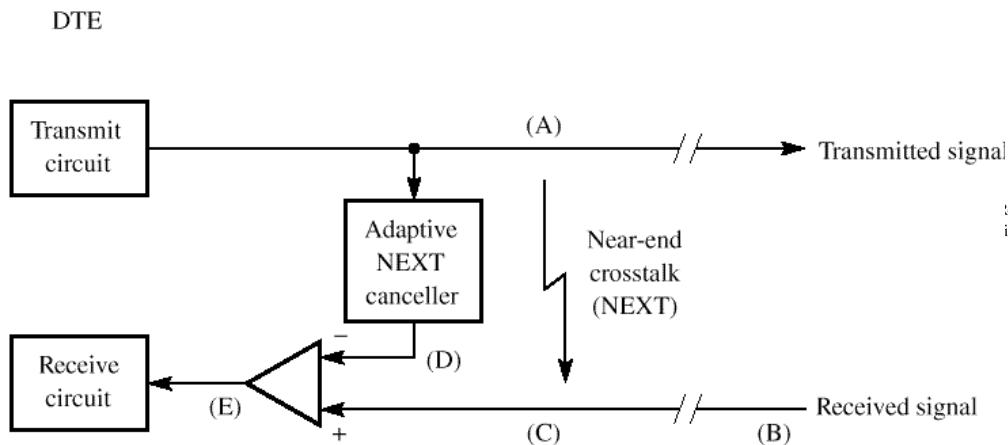
- The effects of noise on channel capacity can be seen using the **Shannon-Hartley Law**:

$$C = B \log_2 \left(1 + \frac{S}{N}\right) \text{bps}$$

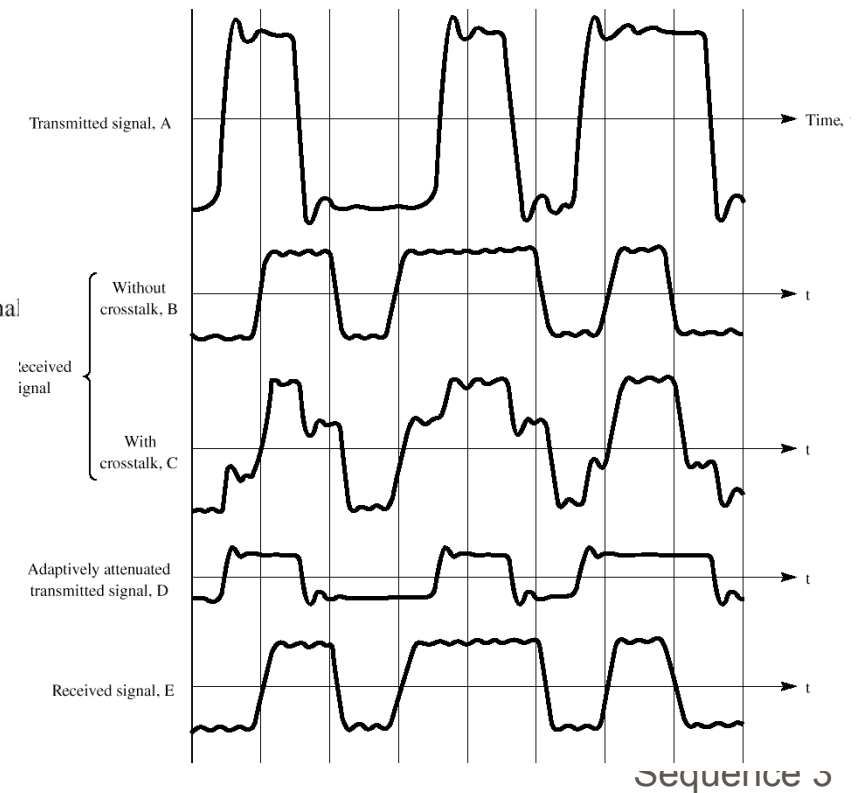
C = data transfer rate in bps
 B = bandwidth (in hertz)

Cross Talk -- NEXT canceling

- near-end crosstalk (NEXT), cross talk of strong transmit (output) signal to weak receive (input) signal.
- adaptive NEXT canceling using op-amp



Hal96 fig.2.9



Noise

- Impulse Noise
 - impulse caused by switching, lightning etc.
- Thermal Noise
 - present irrespective of any external effects
 - caused by thermal agitation of electrons

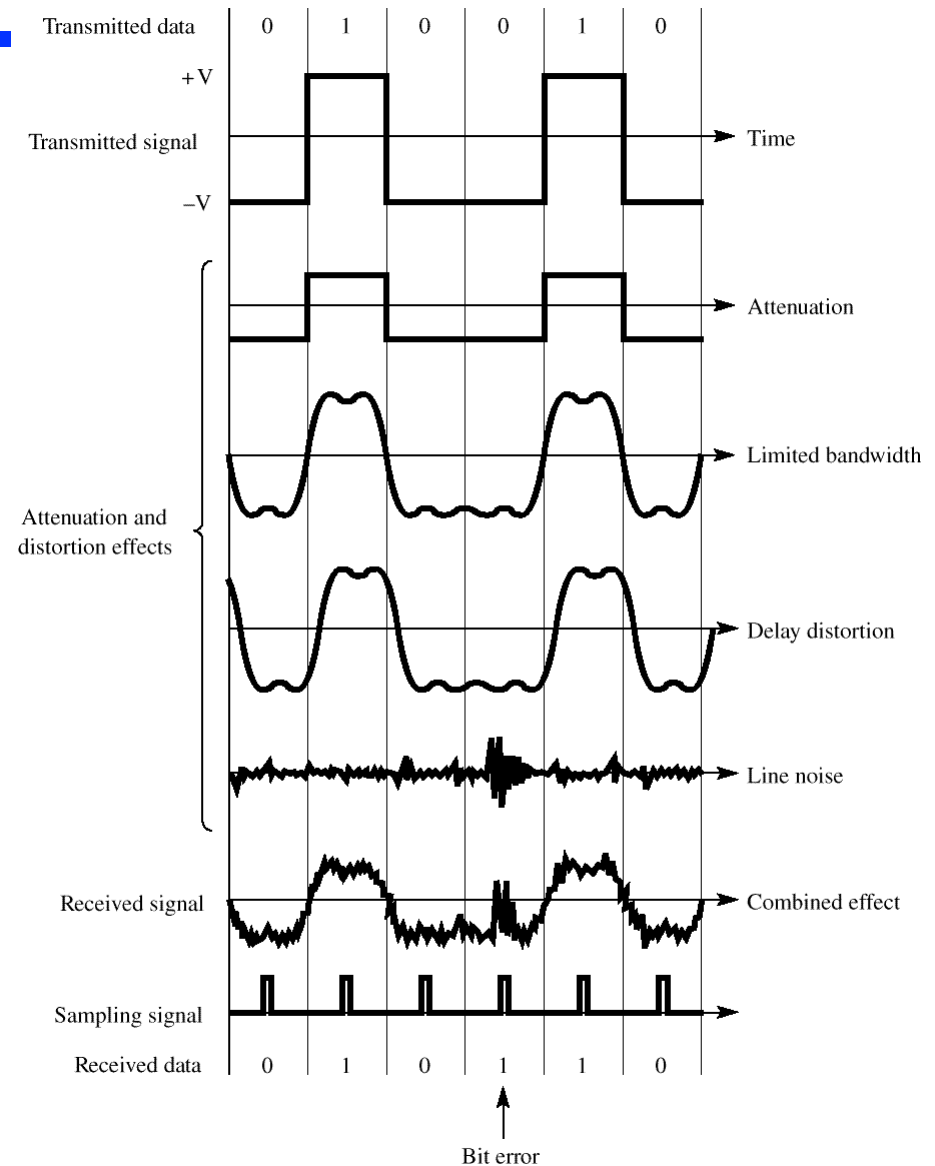
Noise

- White Noise
 - random noise – entire spectrum
- Pink Noise
 - “realistic spectrum”
 - the power spectral density is inversely proportional to the frequency

Combined Effects

- Attenuation
- Limited Bandwidth
- Noise

It all adds up!



Hal96 fig.2.6

Thermal Noise

- Energy (in joules = watts x seconds) per bit in a signal:

$$E_b = ST_b$$

S = signal power in watts

T_b = time period for 1 bit in seconds

- Data Transmission rate $R = 1/T_b$

- Thermal noise N_0 in a line is: (T is temperature in K)

$$N_0 = kTW \text{ where } k = 1.3803 \times 10^{-23} \text{ joule K}^{-1}$$

k is Boltzmann
constant

W is the bandwidth

$$\frac{E_b}{N_0} = \frac{S/R}{N_0} = \frac{S/R}{kTW}$$

Signal Delay

- There exists a **transmission propagation delay** in any medium
 - Speed of light $3 \times 10^8 \text{ ms}^{-1}$
 - Speed of EM in cable/wire $2 \times 10^8 \text{ ms}^{-1}$
- Important parameter is **round-trip-delay** (time from first bit sent to last bit acknowledged)

Signal Delay

—Propagation delay T_p and transmission delay T_x

$$T_P = \frac{d}{V}, \quad T_x = \frac{n}{R}$$

—Important ratio $\frac{T_P}{T_x}$

d = distance in meters
 V = EM speed

n = number of bits transmitted
 R = link bit rate in bits per second