- Absorbing State
  - Simple Triplex System with fail-stop behavior
  - Assumptions:
    - » no repair
    - » perfect fault coverage
      - recall: fault coverage is a measure of the systems ability to detect faults and recover
    - » homogeneous components
    - » independent failures

- System with Repair
  - Simple Triplex System with fail-stop behavior and repair
  - Same assumptions as previous example

- Fault Coverage
  - Simple Triplex System
  - Fault Coverage
  - » C = probability that fault is properly handled
  - »  $C_i$  has major impact on reliability

- Multiple Faults
  - Simple Triplex System with double fault

$$t_r = \text{recovery time from fault}$$

$$\rho = \frac{1}{t_r} \quad \text{recovery rate}$$

- Simple Triplex System with double fault (cont.)

- Different λ's
  - e.g. hot + cold spares
    - » typical MTTF(cold) = 10 MTTF(hot)
  - notation: h.c
    - $\rightarrow$  h = number of hots
    - $\sim$  c = number of colds
  - assume perfect coverage
  - assume switching mechanism

- Passive TMR with 2 Failure Modes
  - fail passive => processor just disconnects
  - notation: n.f
    - » n = number of non-faulty processors running
    - » f = number of faulty processors running
  - assume different fail rates
    - » failure mode 1: benign fail rate  $\lambda_{\text{stop}}$
    - » failure mode 2: single non-benign fail rate  $\lambda_{err}$

Passive TMR with 2 Failure Modes (cont.)

#### Sharpe & Markov Chains

Here we used SHARPE to determine the unreliabilities.

The main slide of interest is the last one that contains the probabilities of being in the specific states.

Why is this interesting? Well...

#### Sharpe & Markov Chains

- SHARPE extracts model and analysis type:
  - Cyclic vs. Acyclic Model
  - Steady-State vs. Transient Analysis

```
markov model_name
{param_list}

from to transition_rate

<name name expression>
end

initial state probabilities

<name expression>
end
```

#### Markov Model

- P(0) = 0 is assumed for any state not listed in initialization
- The sum of all P(0) must be 1
  - » Beware of round-off errors
- Initial state probabilities section may be left empty if:
  - » Acyclic model with only 1 source state
    - Assumes P(0) = 1 for that state
  - » Irreducible model Steady State analysis
    - in this case initial conditions are irrelevant
- Advice: Always specify initial probabilities

#### Useful functions

- tvalue (t; model\_name, state; arg\_list)
  - Gives Transient Probabilities at time t.
  - If no state is given:
    - » computes transient prob. of being in an absorbing state at time t
    - » there can be more than one absorbing state
      - => prob. of being in any absorbing state.
  - If state is given:
    - $\sim$  computes transient prob. of being in that state at time t

#### Useful functions

- prob ( model\_name, state {;arg\_list} )
  - Gives Steady State Probabilities (no time param)
  - Note: state parameter is not optional
  - With absorbing states this computes the steady state probability of ever visiting a specific state
  - If no absorbing states exist (irreducible chain), the steady state probability of being in a specified state is computed

# Interpretation of F(t)

- If a non-absorbing state is specified:
  - F(t) is the transient or steady state CDF for that state
- If an absorbing state is specified:
  - F(t) is the CDF to absorbing by that state
  - absorbing state normally indicates a specific failure mode
- If no state is specified:
  - F(t) is the CDF to include all absorbing states
  - i.e. it is the sum of all CDFs of individual absorbing states
  - e.g. indicating system failure

#### TMR example

```
* SYSTEM: TMR_2MODE -- PASSIVE TMR WITH: FAIL-STOP AND FAIL-ACTIVE MODES
* MODELS: MARKOV (ACYCLIC)
* STATE NOTATION: "N.F" WHERE:
        N == NUMBER OF NON-FAULTY PROCESSORS RUNNING.
        F == NUMBER OF FAULTY PROCESSORS STILL RUNNING.
*----- MODEL DEFINITIONS
MARKOV tmr 2mode
3.0 2.0 3*LAMstop
3.0 2.1 3*LAMerr
2.0 1.0 2*LAMstop
 2.0 1.1 2*LAMerr
2.1 2.0 1*LAMstop
2.1 1.1 2*LAMstop
2.1 1.2 2*LAMerr
1.0 0.0 1*LAMstop
1.0 0.1 1*LAMerr
END
*----- INITIAL CONDITIONS (START IN 3.0)
3.0 1.00
END
```

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#### TMR example

```
----- PARAMETER BINDING
BIND
LAMBDA 1*10^-4
LAMstop 0.9*LAMBDA
LAMerr 0.1*LAMBDA
END
*----- ANALYSES AND EVALUATIONS
cdf (tmr_2mode)
cdf (tmr_2mode,0.0)
var fail01 value(100.0;tmr_2mode,0.1)
var fail11 value(100.0;tmr_2mode,1.1)
var fail12 value(100.0;tmr_2mode,1.2)
var failrun fail01 + fail11 + fail12
var failstop value(100.0;tmr_2mode,0.0)
var failall failrun + failstop
expr fail01
expr fail11
expr fail12
expr failrun
expr failstop
expr failall
END
```

#### TMR example

#### CDF for system tmr\_2mode:

```
1.0000e+00 t( 0) exp( 0.0000e+00 t)
+ -2.5579e+00 t( 0) exp(-1.0000e-04 t)
+ 2.4000e+00 t( 0) exp(-2.0000e-04 t)
+ -2.8421e+00 t( 0) exp(-2.9000e-04 t)
+ 2.0000e+00 t( 0) exp(-3.0000e-04 t)
```

mean: 1.6713e+04 variance: 1.3541e+08

\_\_\_\_\_

information about system tmr\_2mode node 0.0

probability of entering node: 7.5414e-01

conditional CDF for time of reaching this absorbing state

1.0000e+00 t(0) exp(0.0000e+00 t)

- + -3.0526e+00 t(0) exp(-1.0000e-04 t)
- + 3.2222e+00 t( 0) exp(-2.0000e-04 t)
- + -1.1696e+00 t( 0) exp(-2.9000e-04 t)

mean: 1.8448e+04 variance: 1.3689e+08 fail01: 7.9815e-08

. .

fail11: 5.3038e-05

fail12: 2.9416e-06

failrun: 5.6059e-05

-----

failstop: 7.1833e-07

-----

failall: 5.6778e-05