System Diagnosis

- Objective
  - Designing systems that are capable of self-diagnoses of multiple faults
- Motivation
  - Multiprocessor systems employ increasing numbers of processors. Some of these processors will fail.
  - Applications include safety critical systems.
  - Inaccessible systems, e.g. remote, under water or ground, space.
  - "It is always good to know who your enemies are".

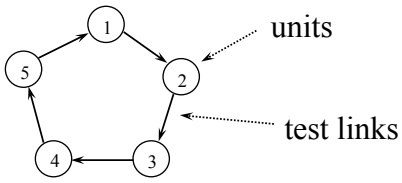
System Diagnosis

- Assumptions
  - System is partitioned into *units*
    - units need not be identical
    - units are powerful enough to test and judge other units pass/fail.
  - Tests are adequate to detect all faults
    - perfect coverage. (This is very restrictive since it also implies faults to be permanent).
  - There exists a reliable method for collecting and evaluating all test results
    - e.g. reliable broadcast
  - These assumptions are often termed *PMC Model*, after early work by Preparata, Metze and Chien (1967)

    "On the Connection Assignment Problem of Diagnosable Systems", IEEE Trans. on Electronic Computers, Vol. EC16, No. 6, Dec. 1967.

System Diagnosis

- System Graph



- Definitions
  - Test graph $G = (U, E)$
  - U : the set of units
  - E : the set of testing links (edges)
  - a_{ij}: the outcome of test (U_i, U_j)

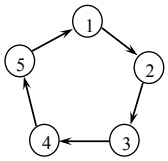
    if U_i is non-faulty then

    if U_j is non-faulty => $a_{ij} = 0$

    if U_j is faulty => $a_{ij} = 1$

    else a_{ij} is unreliable

System Diagnosis



- Example: single fault, U_1 faulty
  - Then $a_{51} = 1$ and $a_{12} = X$ (0 or 1)
  - Syndrome S = set of all outcomes
    - order all a_{ij}

      -> a_{12} -> a_{23} -> a_{34} -> a_{45} -> a_{51} ->^

      -> X -> 0 -> 0 -> 0 -> 1 ->^
  - 2 cases
    - Single 1 in a_{51} => U_1 is faulty
      - note if U_5 was faulty, then $a_{45} = 1$
    - Pair of adjacent 1's
      - the "upstream" 1 is correct
      - $a_{45} = 1$

System Diagnosis

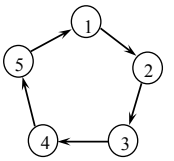
- Definition: t-fault-diagnosable
  - Every set of up-to t faulty units can be correctly diagnosed (eventually).
    - Previous example is 1-fault-diagnosable
    - not 2-fault diagnosable
      - e.g. assume U1 and U2 faulty and $a_{12} = 0$
      - same syndrome as 1-fault-diagnosable example
- Definition: one-step t-fault-diagnosable
  - For every set of up-to *t* faulty units there exists a unique syndrome which correctly identifies <u>all</u> faulty units.

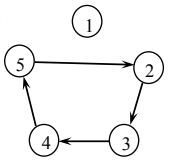
System Diagnosis

- Definition: Sequential t-fault-diagnosable
  - For every set of up-to t faulty units there exists a unique syndrome which correctly identifies at least one faulty unit.
  - (Can be applied recursively)

System Diagnosis

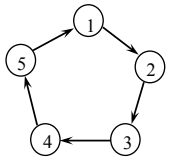
- Example: dual fault
  - Assume U_1 and U_2 are both faulty
    - $(a_{12}, a_{23}, a_{34}, a_{45}, a_{51})$
    - (X , X , 0 , 0 , 1)
  - Could mimic single fault at U_1
    - i.e. (0 , 0 , 0 , 0 , 1)
  - But, pattern 001 always points to a faulty unit
    - thus remove U_1 and reconfigure
    - $(a_{23}, a_{34}, a_{45}, a_{52})$
    - (X , 0 , 0 , 1)
    - still have 001 pattern => U_2 diagnosed to be faulty

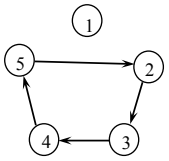




System Diagnosis

- Example: dual fault
  - Assume U_1 and U_3 are both faulty
    - $(a_{12}, a_{23}, a_{34}, a_{45}, a_{51})$
    - (X , 1 , X , 0 , 1)
  - Now possible pattern
    - (1 , 1 , 1 , 0 , 1)
    - still points to one faulty unit => U_1
    - after reconfiguration
      - $(a_{23}, a_{34}, a_{45}, a_{52})$
      - (1 , X , 0 , 0)
    - points to one faulty unit => U_3





System Diagnosis

- Necessary and Sufficient Conditions
  - t = # of faults
  - n = # of units
  - N = # of testing links
  - One-step t-fault-diagnosable system
    $n \geq 2t + 1$
    - each unit is tested by **more** than t-1 other units (or: at least t)
    - this implies $N \geq n \cdot t$
    - optimal: replace $\geq$ with $=$
  - Sequentially t-fault-diagnosable system
    - $n \geq 2t + 1$ ⟵ necessary
    - $N \geq n + 2t - 2$ ⟵ and sufficient

System Diagnosis

- Single Loop System (Ring)
  - Let $t = 2m + \lambda$
    (m: integer; λ: 0 or 1 (even or odd))
  - Loop is sequentially t-fault-diagnosable if
    $n \geq 1 + (m+1)^2 + \lambda(m+1)$
    - proof given in paper Pre67
  - e.g.
    - $t = 1 \Rightarrow \quad m = 0, \quad \lambda = 1, \qquad n = 1 + 1 + 1 = 3$
    - $t = 2 \Rightarrow \quad m = 1, \quad \lambda = 0, \qquad n = 1 + 2^2 + 0 = 5$
    - $t = 3 \Rightarrow \quad m = 1, \quad \lambda = 1, \qquad n = 1 + 2^2 + 2 = 7$

System Diagnosis

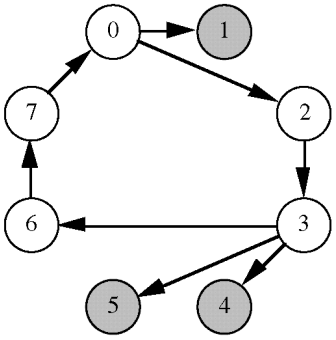
- Inefficiency of PMC
  - PMC requires for t-diagnosability, that each node must be tested by at least t other nodes.
  - Problem: many diagnosis!
  - Alternative: adaptive models
    - the term adaptive stems from allowing the choice of which test(s) to perform depend on the results of previous tests.

System Diagnosis

- Adaptive Distributed System Diagnosis
  - "Implementation of On-Line Distributed System-Level Diagnosis Theory" by Bianchini and Buskens, Trans. on Computers, May 1992
  - Uses array TESTED_UP$_x$ at each node n_x
  - Meaning of TESTED_UP$_x$[i]
    - TESTED_UP$_x$[i] = j implies that node n_x has received information from fault-free node n_i, that n_i found n_j to be fault-free.
  - Idea:
    - each node finds first node that is fault-free
      - n_i checks n_j $j > i$ mod N, where N is the number of nodes.
    - get other TESTED_UP$_i$ values from TESTED_UP$_j$
    - implies that node n_x has received information from fault-free node n_j, that n_i found n_j to be fault-free.

System Diagnosis

Example: assume nodes 1, 4 and 5 are faulty



TESTED_UP$_2$[0] =	2
TESTED_UP$_2$[1] =	x
TESTED_UP$_2$[2] =	3
TESTED_UP$_2$[3] =	6
TESTED_UP$_2$[4] =	x
TESTED_UP$_2$[5] =	x
TESTED_UP$_2$[6] =	7
TESTED_UP$_2$[7] =	0

Bia92, fig 4 and 6

System Diagnosis

- Adaptive Distr.Sys.Diag. Algorithm (Bia92 fig 5)

```
        /* ADAPTIVE_DSD                                                    */
        /* The following is executed at each n_x, 0 ≤ x ≤ N-1 at predefined */
        /* testing intervals.                                              */
1.      y = x;
2.      repeat {
2.1.            y = (y + 1) mod N;
2.2.            request n_y to forward TESTED_UP_y to n_x;
2.3.    } until (n_x tests n_y as "fault-free");
3.      TESTED_UP_x[x] = y;
4.      for i = 0 to N-1
4.1.            if (i ≠ x)
4.1.1.                  TESTED_UP_x[i] = TESTED_UP_y[i];
```

request issued before node is tested fault-free => keep data only if n_y ok

(Bia92 fig 5)

System Diagnosis

- Diagnosis
  - accomplished at any node n_x by following the fault-free paths from n_x to other fault-free nodes.

```
        /* DIAGNOSE                                                    */
        /* The following is executed at each n_x, 0 ≤ x ≤ N-1 when n_x */
        /* desires diagnosis of the system.                            */
1.      for i = 0 to N-1
1.1.            STATE_x[i] = faulty;
2.      node_pointer = x;
3.      repeat {
3.1.            STATE_x[node_pointer] = fault-free;
3.2.            node_pointer = TESTED_UP_x[node_pointer];
3.3.    } until (node_pointer == x);
```

Bia92 fig. 7