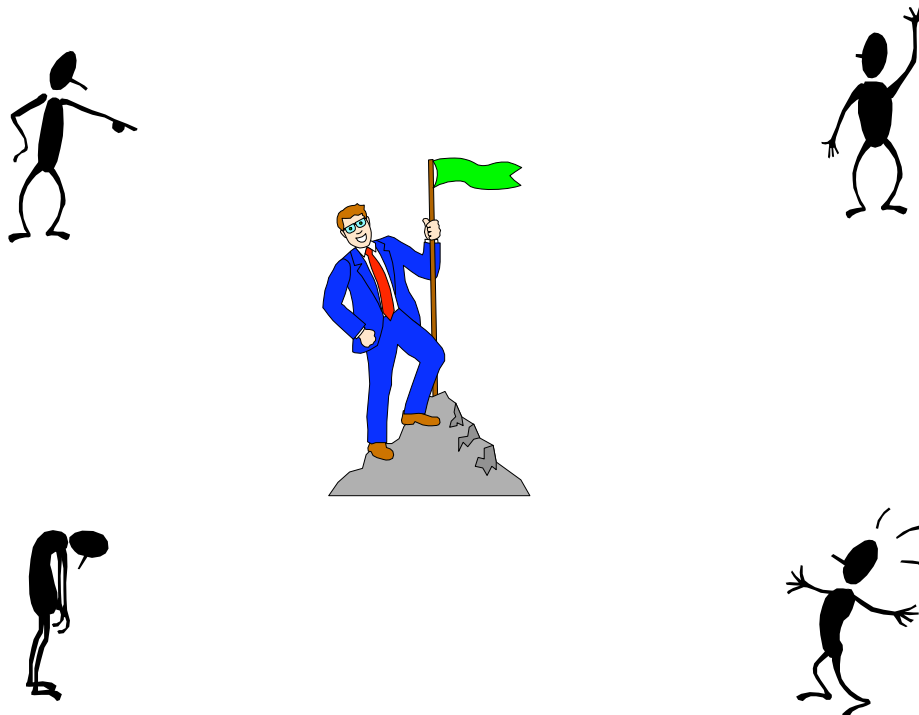


# *Introduction FT Agreement*

- ◆ We will discuss fault tolerant agreement algorithms during this class.
- ◆ We want to start out the discussion with the Byzantine General Problem
  - L. Lamport, R. Shostak, and M Pease, "The Byzantine Generals Problem"
- ◆ Variations of the problem will follow us throughout the rest of the semester.
- ◆ What started it all?
  - Clock synchronization problems in SIFT

## *Byzantine General Problem*



# *Byzantine General Problem*

- ◆ Objective
  - A) All loyal generals must decide on the same plan of action
  - B) A “small” number of traitors cannot cause the loyal generals to adopt a “bad” plan.
- ◆ Types of agreement
  - exact agreement
  - approximate agreement
- ◆ Applications, e.g.
  - agreement in the presence of faults
  - event, clock synchronization

# *Byzantine General Problem*

- ◆ Key to disagreement
  - 1) Initial disagreement among loyal generals
  - 2) Ability of traitor to send conflicting messages
    - » asymmetry
- ◆ Reduction of general problem to simplex problem with 1 General and n-1 Lieutenants
  - General gives order
  - Loyal Lieutenants must take single action

## *Byz. Gen. Prob. (Simplex)*

### ◆ Want

IC1: All loyal Lieutenants obey the same order

IC2: If the commanding General is loyal, the every loyal Lieutenant obeys the order he sends

- IC1 & IC2 are called *Interactive Consistency Conditions*.
- If the General is loyal, then IC1 follows from IC2.
- However, the General need not be loyal.

### ◆ Any solution to the simplex problem will also work for multiple-source problems.

- the  $i^{th}$  General sends his value  $v(i)$  by using a solution to the BGP to send the order “use  $v(i)$  as my value”, with the other Generals acting as the lieutenants.

## *BGP: Oral Message Solution*

### ◆ Oral Message

- message whose contents are under the control of the sender (possibly relays)

### ◆ Practical implication, sensor example

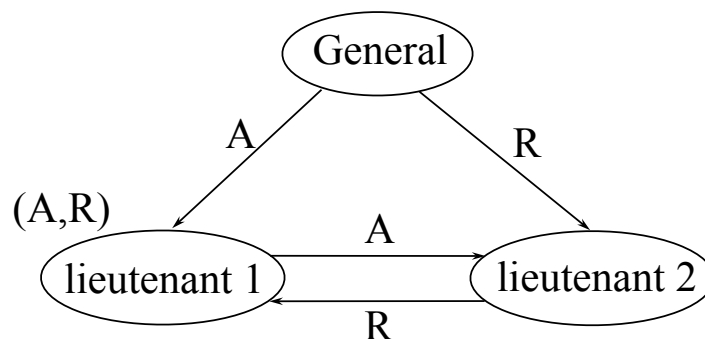
- General = sensor
- Lieutenants = processor redundantly reading sensor
- Initial disagreement
  - » time skew in reading, bad link to sensor
  - » analog - digital conversion error, any threshold function
- Asymmetry
  - » communication problem, noise, V-level, bit timing

## *BGP: Oral Message Solution*

- ◆ The Byzantine Generals Problem seems deceptively simple, however
- ◆ no solution will work unless more than two-third of the generals are loyal.
- ◆ Thus, there exists no 3-General solutions to the single traitor problem using oral messages
- ◆ Assume the messages sent are
  - A = Attack
  - R = Retreat

## *BGP: Oral Message Solution*

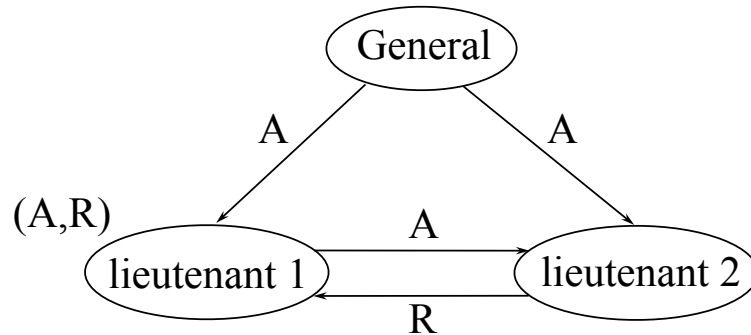
- ◆ Case 1: Commander is traitor:



- commander is lying
- who does lieutenant 1 believe
- could pick default

## *BGP: Oral Message Solution*

- ◆ Case 2: Lieutenant 2 is traitor:



- lieutenant 2 is lying
- who does lieutenant 1 believe
- could pick default, but what if it is R
  - » then General has A and Lieutenant 1 has R !!!

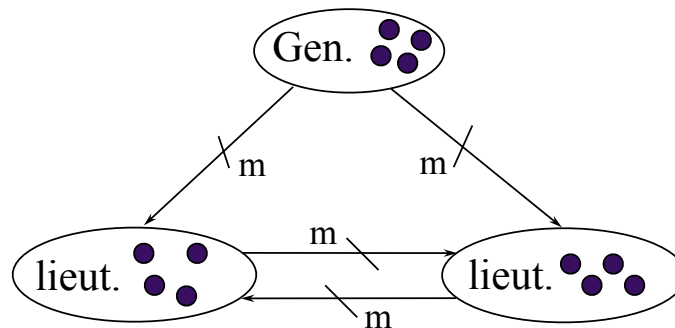
## *BGP: Oral Message Solution*

- ◆ Given case 1 and case 2, lieutenant 1 cannot differentiate between both scenarios, i.e. the set of values lieutenant 1 has is (A,R).
- ◆ In general: Given  $m$  traitors, there exists no solution with less than  $3m+1$  generals for the oral message scenario.
- ◆ Assumptions about Oral Messages
  - every message that is sent is delivered correctly
  - the receiver of a message knows who send it
  - the absence of a message can be detected
  - how realistic are these assumptions?

# BGP: Oral Message Solution

## ◆ General case:

- regroup generals
  - »  $n$  Albanian generals
  - »  $n/3$  act as unit  $\Rightarrow$  3 general Byzantine General Problem



# BGP: Oral Message Solution

## Algorithm OM(0)

- 1) The commander sends his value to every lieutenant
- 2) Each lieutenant uses the value he receives from the commander, or uses the value RETREAT if he receives no value

## Algorithm OM(m), $m > 0$

- 1) The commander sends his value to every lieutenant.
- 2) For each  $i$ , let  $v_i$  be the value lieutenant  $i$  receives from the commander, or else be RETREAT if he receives no value. Lieutenant  $i$  acts as the commander in Algorithm OM(m-1) to send the value  $v_i$  to each of the  $n-2$  other lieutenants.
- 3) For each  $i$ , and each  $j \neq i$ , let  $v_j$  be the value lieutenant  $i$  received from lieutenant  $j$  in step 2) (using algorithm OM(m-1), or else RETREAT if he received no such value. Lieutenant  $i$  uses the value

$$\text{majority}(v_1, \dots, v_{n-1})$$

# BGP: Oral Message Solution

OM(m) -- same thing, different wording

IF  $m = 0$  THEN

- a) commander sends his value to all other  $(n-1)$  lieutenants.
- b) lieutenant uses value received or default (i.e. RETREAT if no value was received).

ELSE

- a) each commander node sends value to all other  $(n-1)$  lieutenants
- b) let  $v_i$  = value received by lieut.  $i$  (from commander OR default if there was no message)

Lieut.  $i$  invokes OM( $m-1$ ) as commander, sending  $v_i$  to other  $(n-2)$  lieutenants.

- c) let  $v_{ji}$  = value received from lieutenant  $j$  by lieutenant  $i$ .

Each lieutenant  $i$  gets  $v_i = \text{maj}(\text{what everyone said } j \text{ said in prev.round, except } j \text{ himself})$

trust myself more than  
what others say I said

## example $n=4 \Rightarrow$ one traitor

### ◆ procedure OM(1)

IF {not valid since  $m=1$ }

ELSE

- 1) commander transmits to L1,L2,L3
- 2) values are received by L1,L2,L3  
so lieuts call OM(0)

each lieut has  
received 3 values  
(use majority)

procedure OM(0)  
IF { $m=0$ }  
1) each lieut sends value to  
other 2 lieuts  
ELSE {not valid}

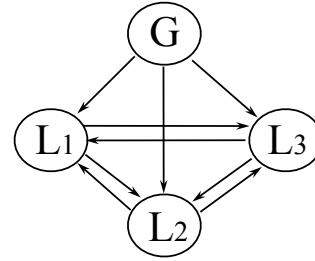
# BGP example

◆ case 1: L3 is traitor

$v_0 = 1$

each loyal L has vector

110 or 111  $\Rightarrow \text{maj}(1\ 1\ 0/1) = 1$



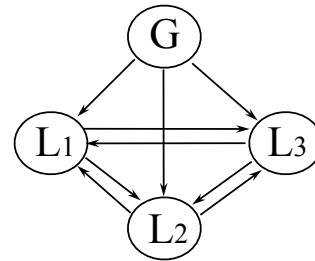
◆ case 2: G is traitor

$v_0 \Rightarrow L1=1\ L2=1\ L3=0$

L1 has 110

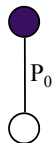
L2 has 110  $\text{maj}() = 1$

L3 has 011

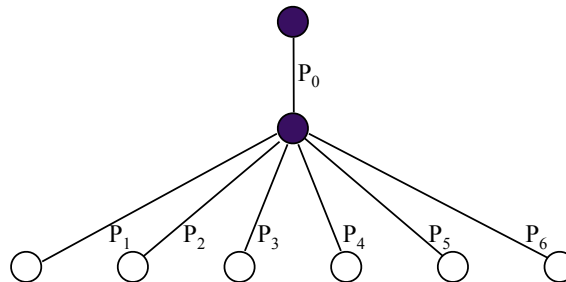


# BGP with $N = 7$

General sends message

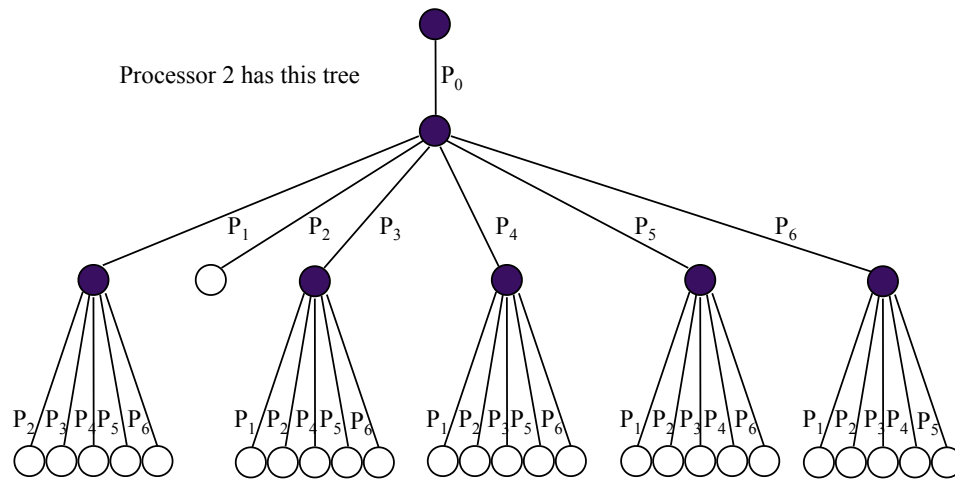


After first rebroadcast





# *BGP with $N = 7$*



# *BGP with $N = 3m + 1$*

extra blank

# *BGP with $N = 7$*

