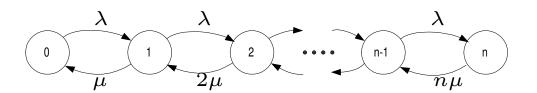
- This section discusses an approach to eliminate the fail-rate in the determination of survivability.
- Source of presentation:
 - A General Framework for Network Survivability Quantification,
 - by Yun Liu and Kishor S. Trivedi,
 - in Proceedings of the 12th GI/ITG Conference on Measuring,
 Modelling and Evaluation of Computer and Communication Systems
 (MMB) together with 3rd Polish-German Teletraffic Symposium
 (PGTS), Dresden, Germany, September 2004.
- Application is telecommunication switching system
- The material of the slides are directly drawn from the paper

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Survivability Quantification

- Pure Performance Markov Model
 - *n* trunks (channels) with an infinite caller population
 - call arrival process is assumed to be Poisson with rate λ
 - exponentially distributed holding times with rate μ
 - Markov chain shows i ongoing calls presented in state i
 - what does it mean to be in state *n*: system handling *n* calls, but blocks for all newly arriving calls



- Performance
 - What is the measure of performance?
 - Blocking probability P_{bk}
 - » the probability that all *n* channels are occupied
 - » consider steady state probability of being in state j

$$\pi_j^P = \frac{(\frac{\lambda}{\mu})^j / j!}{\sum_{k=0}^n (\frac{\lambda}{\mu})^k / k!}$$

» then blocking probability is

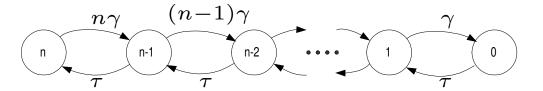
$$P_{bk} = \pi_n^P$$

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Survivability Quantification

- Pure Availability Markov Model
 - *n* trunks (channels) with an infinite caller population
 - failure rate γ
 - repair rate τ
 - state *i* indicates that there are *i* non-faulty channels in the system
 - what does it mean to be in state 0: system is unavailable



- Availability
 - What is the measure of availability?
 - Steady state probability of state *i* in pure availability model:

$$\pi_i^A = \frac{(\frac{\tau}{\gamma})^i / i!}{\sum_{k=0}^n (\frac{\tau}{\gamma})^k / k!}$$

- probability of all channels down is

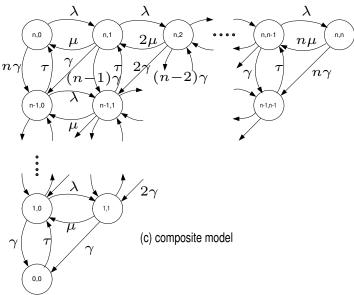
$$P_A = \pi_0^A$$

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Composite Markov Model

State (i,j) indicates that there are i non-failed channels in the system and j of them are carrying ongoing calls



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- Performability
 - What is the measure of performance in this combined model?
 - Blocking probability $P_{bk}^{'}$
 - » the probability that all *n* channels are occupied in any "row" of the chain
 - » this is the diagonal in the 2-dimensional chain
 - » let the steady state probability of state (k,k) be denoted by

$$\pi_{k,k}^{C}$$

» then

$$P'_{bk} = \sum_{k=0}^{n} \pi_{k,k}^{C}$$

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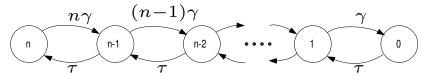
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Survivability Quantification

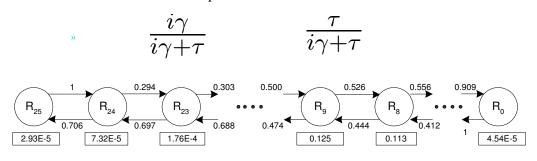
- Survivability definition of Knight et.al.
- A survivability specification is a four-tuple, {E, R, P, M} where:
 - E is a statement of the assumed operating environment for the system
 - R is a set of specifications each of which is a complete statement of a tolerable form of service that the system must provide.
 - P is a probability distribution across the set of specifications, R.
 - M is a finite-state machine denoted by the four-tuple {S,s0,V,T} where S is a finite set of states each of which has a unique label which is one of the specifications defined in R; s0 (s0 ∈ S) is the initial or preferred state for the machine; V is a finite set of customer values; T is a state transition matrix.

Survivability Specification

- Service specification $R(R_n, ..., R_i, ..., R_0)$
 - determined by the number of available trunks i, i=n,...,0



- what are the transition probabilities from state i to i+1 or i-1



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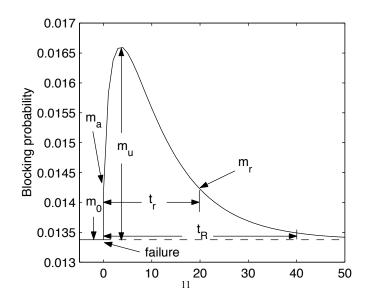
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T1A1.2 Model

- Definition 3.
- Suppose a measure of interest M has the value m0 just before a failure happens. The survivability behavior can be depicted by the following attributes: ma is the value of M just after the failure occurs, mu is the maximum difference between the value of M and ma after the failure, mr is the restored value of M after some time tr, and tR is the time for the system to restore the value m0.

Survivability after 1st Failure

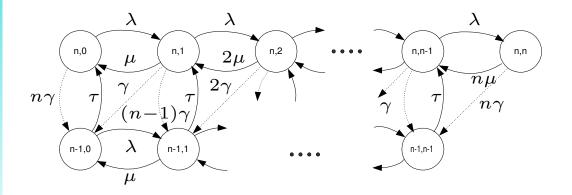
 Based on T1A1.2 definition: Note that it does not matter when the failure occurs.



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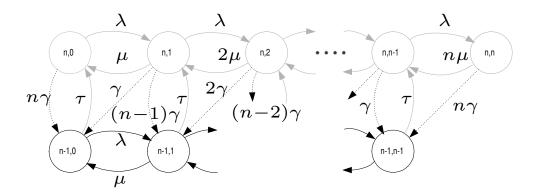
T1A1.2 Markov Model

- Shown is the portion of the previous chain where only the first failure is considered
 - this represents the T1A1.2 model



Truncated composite model

- Model is without repair
 - grey circles and arc represent the removed states and transitions
 - dotted arcs indicate instantaneous transitions have taken place
 - » initial probabilities are from truncated composite model



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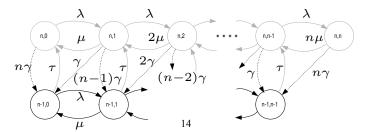
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Truncated composite model

- What are the probabilities of begin in a state *i,j* ?
 - since failure has already happened $p_{n,j}^o = 0$
 - and

$$p_{n-1,j}^o = \frac{n-j}{n} \pi_j^P + \frac{j+1}{n} \pi_{j+1}^P$$

- since state (n-1,j) can be reached from
 - » state (n,j) with transition rate (n-j) γ
 - » state (n,j+1) with transition rate (j+1) γ
 - » note there is no γ left in this expression! Why?



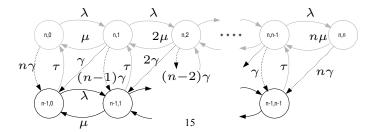
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Truncated composite model

Thus blocking probability is

$$P_{bk}(t) = p_{n-1, n-1}(t) + p_{n, n}(t)$$

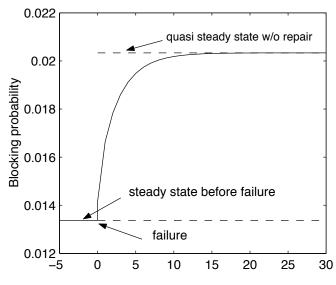
- where $p_{n-1, n-1}(t)$ and $p_{n, n}(t)$ are the transient probabilities of state (n-1, n-1) and (n, n) in the truncated composite model



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Truncated composite model

Survivability after 1st failure without repair



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- The model is then extended to consider more that one (first) faults.
- Note that the approach of the paper overcomes the problems associated with fail-rates, i.e. what is the fail-rate in a survivable system?

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