

## **Chapter 3: Data Transmission**

## **Terminology (1)**

- Transmitter
- Receiver
- Medium
  - Guided medium
    - e.g. twisted pair, coaxial cable, optical fiber
  - Unguided medium
    - e.g. air, seawater, vacuum

## **Terminology (2)**

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- Direct link
  - No intermediate devices
- Point-to-point
  - Direct link
  - Only 2 devices share link
- Multi-point
  - More than two devices share the link

## **Terminology (3)**

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- Simplex
  - One direction
  - One side transmits, the other receives
    - e.g. Television
- Half duplex
  - Either direction, but only one way at a time
    - e.g. police radio
- Full duplex
  - Both stations may transmit simultaneously
  - Medium carries signals in both direction at same time
    - e.g. telephone

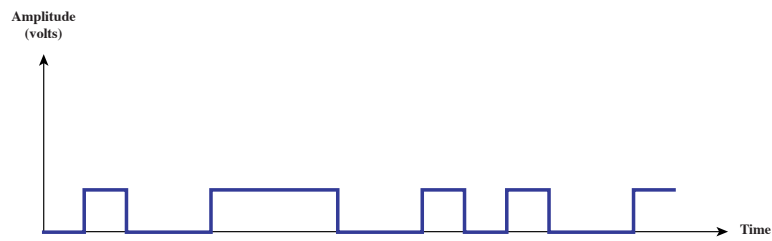
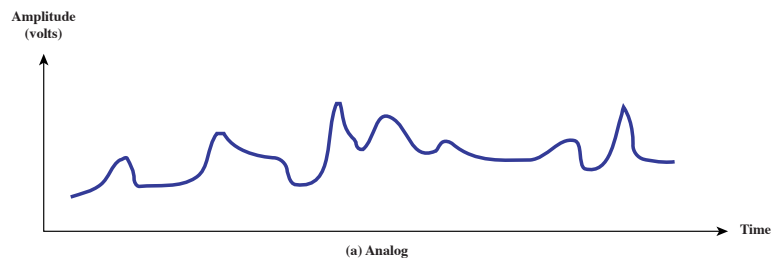
# Frequency, Spectrum and Bandwidth

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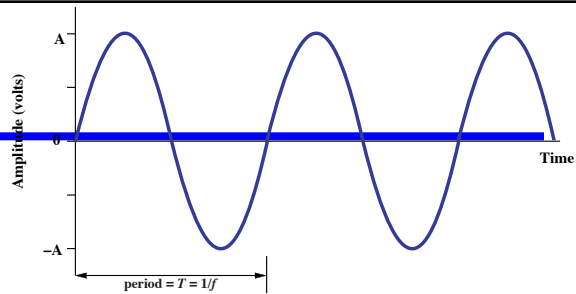
- Time domain concepts
  - Analog signal
    - Varies in a smooth way over time
  - Digital signal
    - Maintains a constant level then changes to another constant level
  - Periodic signal
    - Pattern repeated over time
  - Aperiodic signal
    - Pattern not repeated over time

# Analogue & Digital Signals

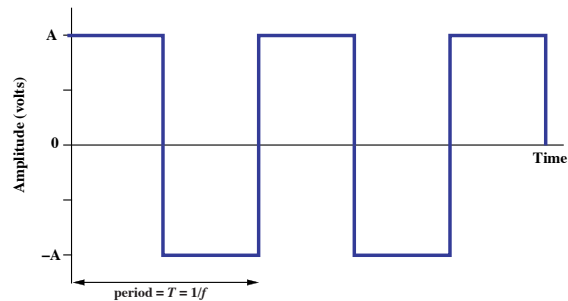
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# Periodic Signals



(a) Sine wave

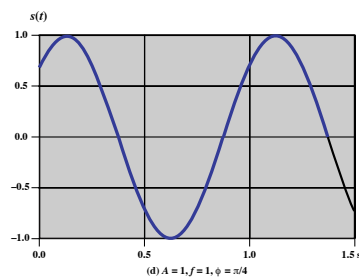
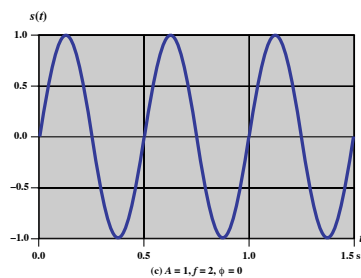
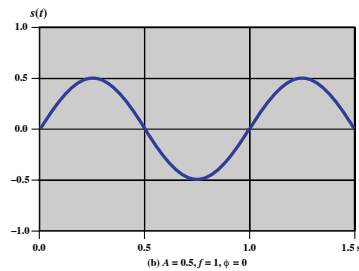
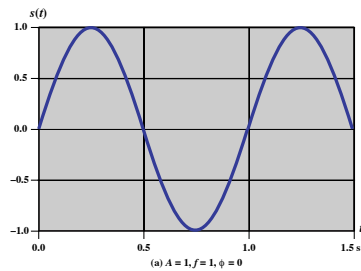


(b) Square wave

## Sine Wave

- Peak Amplitude ( $A$ )
  - maximum strength of signal, in volts
- Frequency ( $f$ )
  - Rate of change of signal, in Hertz (Hz) or cycles per second
  - Period ( $T$ ): time for one repetition,  $T = 1/f$
- Phase ( $\phi$ )
  - Relative position in time
- Periodic signal  $s(t + T) = s(t)$
- General wave  $s(t) = A \sin(2\pi ft + \Phi)$

## Periodic Signal: e.g. Sine Waves

$$s(t) = A \sin(2\pi ft + \Phi)$$


## Wavelength

- Distance occupied by one cycle
- Distance between two points of corresponding phase in two consecutive cycles
- Wavelength  $\lambda$
- Assuming signal velocity  $v$

$$\lambda = vT \quad [\text{unit is m}]$$

$$\lambda f = v$$

$$c = 3 \cdot 10^8 \text{ m/s (speed of light in free space)}$$

## Frequency Domain Concepts

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- Signal is usually made up of many frequencies
- Components are sine waves
- It can be shown (Fourier analysis) that any signal is made up of component sine waves
- One can plot frequency domain functions

## Building block for waves

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- What is a square wave?
  - What frequency components are digital signals composed of?
  - How many components do I need to recreate a square wave?
  - What is a realistic spectrum?
  - Where is the main energy of the signal?
  - Below is a representation of a square wave with amplitude A:

$$s(t) = \frac{A}{\pi} \sum_{k \text{ odd}, k=1}^{\infty} \frac{1}{k} \sin(2\pi kft)$$

## Physical Aspects

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- Limited Bandwidth

- Fourier Analysis

$$v(t) = a_0 + \sum_{n=1}^{\infty} a_n \cos n\omega_0 t + \sum_{n=1}^{\infty} b_n \sin n\omega_0 t$$

$$a_0 = \frac{1}{T} \int_0^T v(t) dt$$

$$a_n = \frac{2}{T} \int_0^T v(t) \cos(n\omega_0 t) dt$$

$$b_n = \frac{2}{T} \int_0^T v(t) \sin(n\omega_0 t) dt$$

$v(t)$  = voltage as a function of time

$\omega_0$  = fundamental frequency component in radians / second

$f_0$  = fundamental frequency in Hz

$T = 1/f_0$  = period in seconds

## Physical Aspects

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- Limited Bandwidth (cont.)

- Unipolar

$$v(t) = \frac{V}{2} + \frac{2V}{\pi} \left\{ \cos \omega_0 t - \frac{1}{3} \cos 3\omega_0 t + \frac{1}{5} \cos 5\omega_0 t - \dots \right\}$$

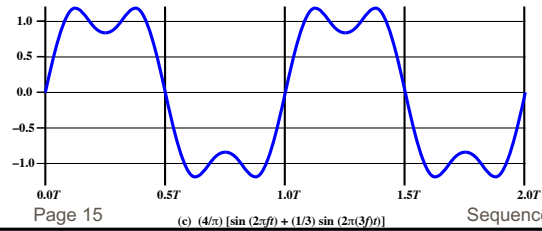
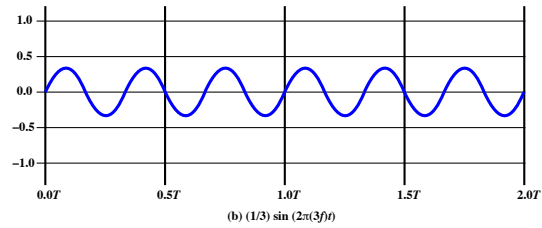
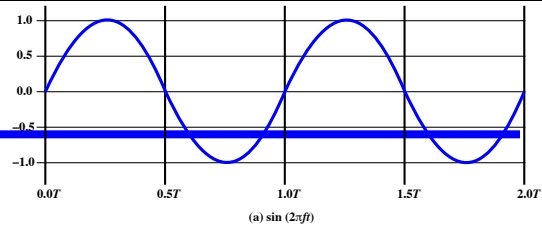
- Bipolar

$$v(t) = \frac{4V}{\pi} \left\{ \cos \omega_0 t - \frac{1}{3} \cos 3\omega_0 t + \frac{1}{5} \cos 5\omega_0 t - \dots \right\}$$

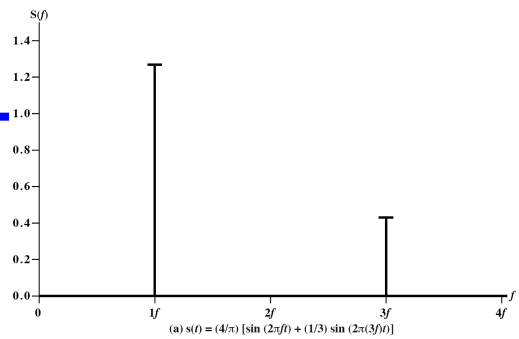
How much bandwidth do we need?

What are the trade-offs if we compromise bandwidth?

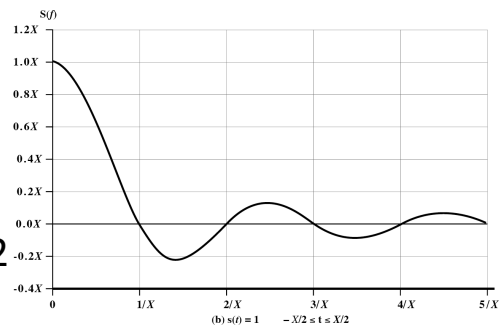
# Addition of Frequency Components (T=1/f)



# Spectrum of previous example



# Single pulse: between $-X/2$ and $X/2$

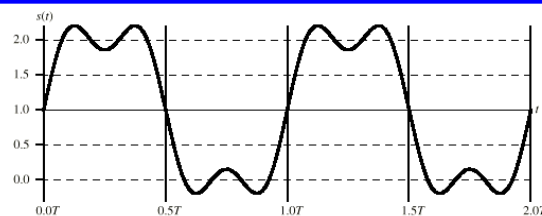




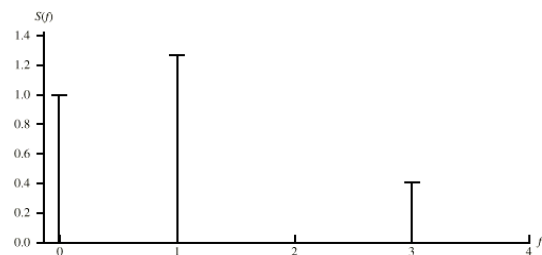
## Spectrum & Bandwidth

- Spectrum
  - range of frequencies contained in signal
- Absolute bandwidth
  - width of spectrum
- Effective bandwidth
  - Often just *bandwidth*
  - Narrow band of frequencies containing most of the energy
- DC Component
  - Component of zero frequency

## Signal with DC Component



$$(a) s(t) = 1 + (4/3) [\sin(2\pi ft) + (1/3) \sin(2\pi 3ft)]$$



(b)  $S(f)$

## **Data Rate and Bandwidth**

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- Any transmission system has a limited band of frequencies
- This limits the data rate that can be carried
- Issues
  - The more bandwidth the less distortion
  - Where is the bulk of the energy?

## **Analog and Digital Data Transmission**

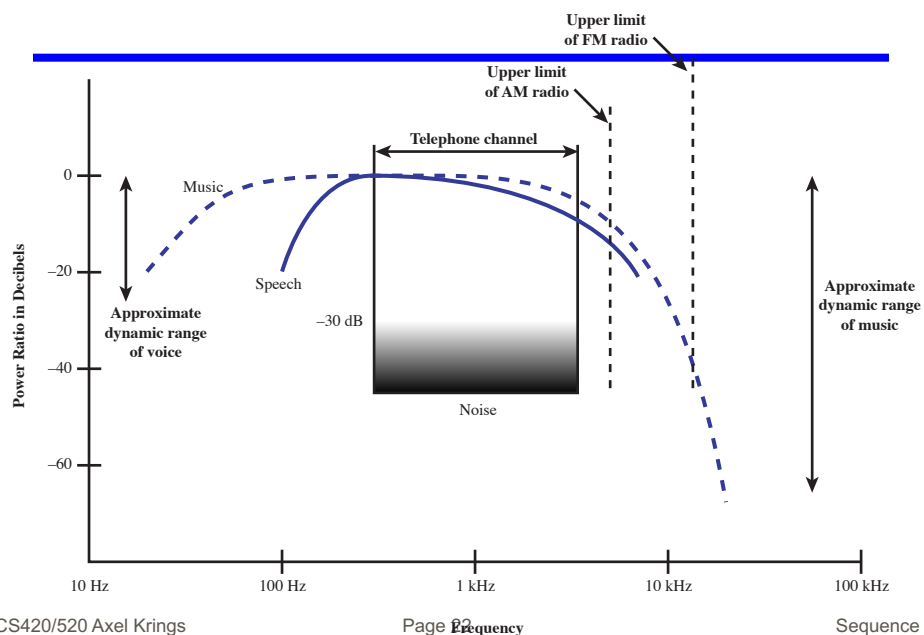
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- Data
  - Entities that convey meaning
- Signals
  - Electric or electromagnetic representations of data
- Transmission
  - Communication of data by propagation and processing of signals

## Analog and Digital Data

- Analog
  - Continuous values within some interval
  - e.g. sound, video
- Digital
  - Discrete values
  - e.g. text, integers

## Acoustic Spectrum (Analog)



## **Analog and Digital Signals**

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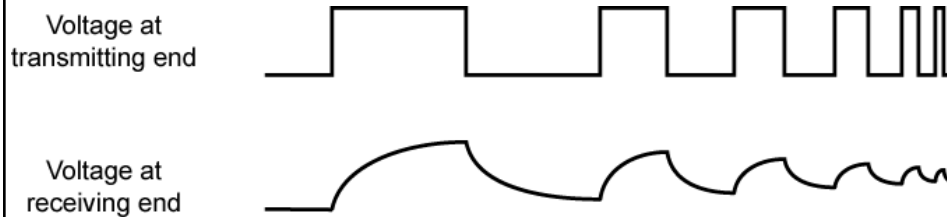
- Means by which data are propagated
- Analog
  - Continuously variable
  - Various media
    - wire, fiber optic, space
  - Speech bandwidth 100Hz to 7kHz
  - Telephone bandwidth 300Hz to 3400Hz
  - Video bandwidth 4MHz
- Digital
  - Use two DC components

## **Advantages & Disadvantages of Digital**

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- Cheaper
- Less susceptible to noise
- Greater attenuation
  - Pulses become rounded and smaller
  - Leads to loss of information

## Attenuation of Digital Signals

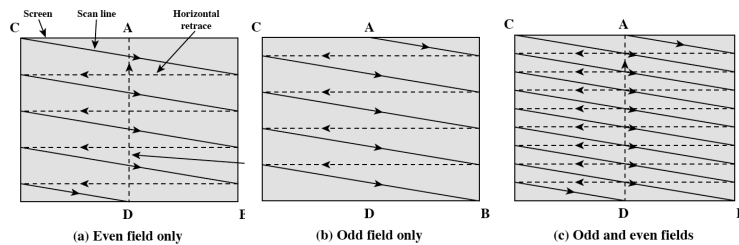


## Components of Speech

- Frequency range (of hearing) 20Hz-20kHz
  - This upper bound is over-optimistic though!
  - Speech 100Hz-7kHz
- Easily converted into electromagnetic signal for transmission
- Sound frequencies with varying volume converted into electromagnetic frequencies with varying voltage
- Limit frequency range for voice channel
  - 300-3400Hz

## Video Components

- USA - 483 lines scanned per frame at 30 frames per second
  - 525 lines but 42 lost during vertical retrace
- So 525 lines x 30 scans = 15750 lines per second
  - 63.5 $\mu$ s per line, (11 $\mu$ s for retrace, so 52.5  $\mu$ s per video line)
- Max frequency if line alternates black and white
- Horizontal resolution is about 450 lines giving 225 cycles of wave in 52.5  $\mu$ s
- Max frequency of 4.2MHz



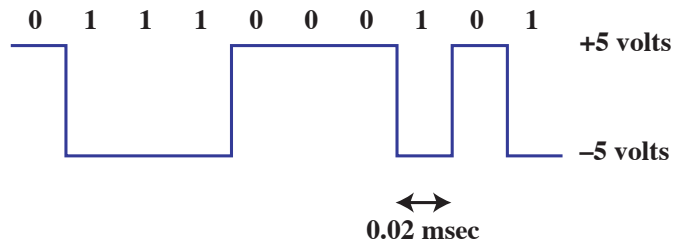
## Binary Digital Data

- From computer terminals etc.
- Two dc components
- Bandwidth depends on data rate

## Conversion of PC Input to Digital Signal

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- as generated by computers etc.
- has two dc components
- bandwidth depends on data rate



User input at a PC is converted into a stream of binary digits (1s and 0s). In this graph of a typical digital signal, binary one is represented by -5 volts and binary zero is represented by +5 volts. The signal for each bit has a duration of 0.02 msec, giving a data rate of 50,000 bits per second (50 kbps).

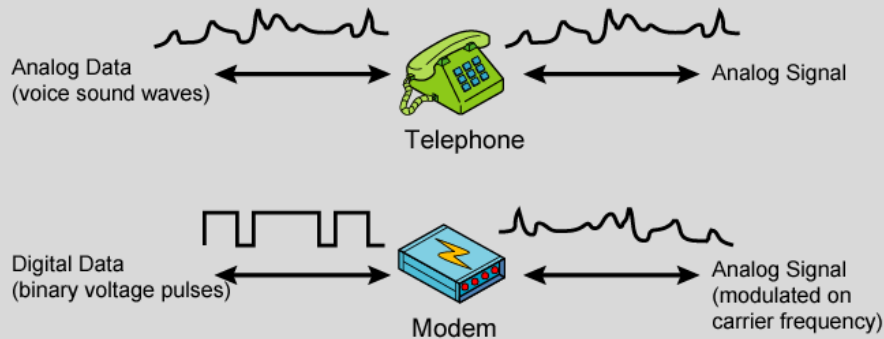
## Data and Signals

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- Usually use digital signals for digital data and analog signals for analog data
- Can use analog signal to carry digital data
  - Modem
- Can use digital signal to carry analog data
  - Compact Disc audio

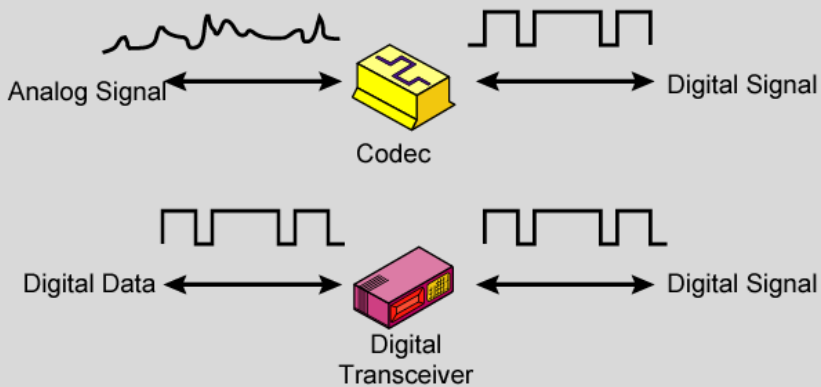
# Analog Signals Carrying Analog and Digital Data

Analog Signals: Represent data with continuously varying electromagnetic wave



# Digital Signals Carrying Analog and Digital Data

Digital Signals: Represent data with sequence of voltage pulses





## **Transmission Impairments**

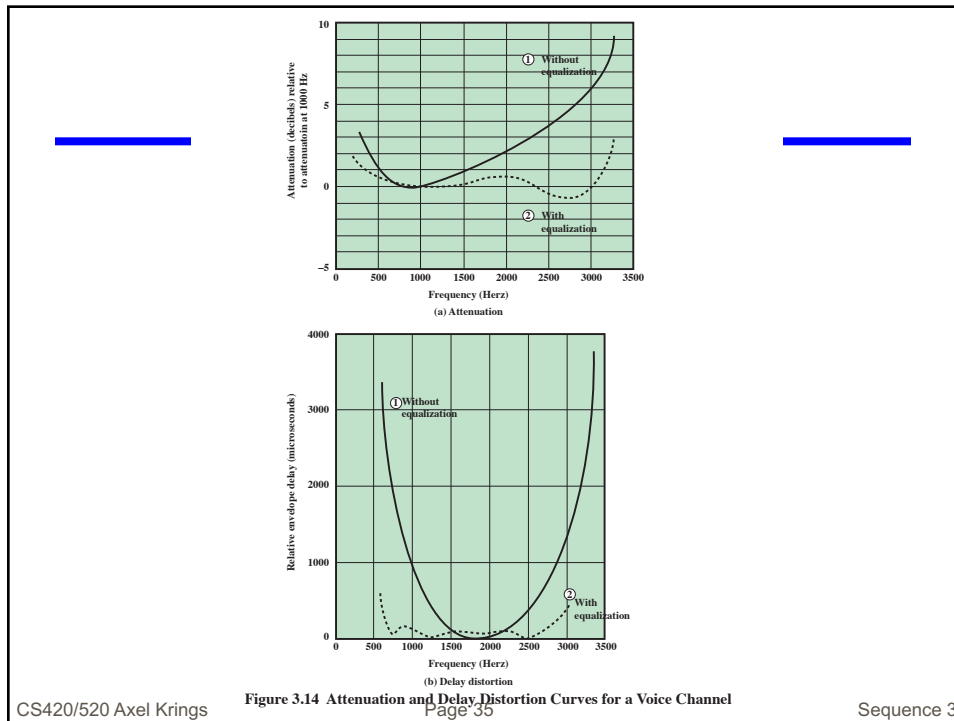
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- Signal received may differ from signal transmitted causing:
  - analog - degradation of signal quality
  - digital - bit errors
- Most significant impairments are
  - attenuation and attenuation distortion
  - delay distortion
  - noise

## **Attenuation**

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- Signal strength falls off with distance
- Depends on medium
- Received signal strength:
  - must be enough to be detected
  - must be sufficiently higher than noise to be received without error
- Attenuation is an increasing function of frequency



## Noise (1)

- Additional signals inserted between transmitter and receiver
- Thermal
  - Due to thermal agitation of electrons
  - Uniformly distributed
  - White noise
- Intermodulation
  - Signals that are the sum and difference of original frequencies sharing a medium

## **Noise (2)**

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- Crosstalk
  - A signal from one line is picked up by another
- Impulse
  - Irregular pulses or spikes
  - e.g. External electromagnetic interference
  - Short duration
  - High amplitude

## **Digital Transmission**

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- Concerned with content
- Integrity endangered by noise, attenuation etc.
- Repeaters
  - Repeater receives signal
  - Extracts bit pattern
  - Retransmits
  - Attenuation is overcome
  - Noise is not amplified

## **Analog Transmission**

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- Analog signal transmitted without regard to content
- May be analog or digital data
- Attenuated over distance
- Use amplifiers to boost signal
- Also amplifies noise

## **Advantages of Digital Transmission**

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- Digital technology
  - Low cost LSI/VLSI technology
- Data integrity
  - Longer distances over lower quality lines
- Capacity utilization
  - High bandwidth links economical
  - High degree of multiplexing easier with digital techniques
- Security & Privacy
  - Encryption
- Integration
  - Can treat analog and digital data similarly

## Delay Distortion

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- Different frequency components of a signal
  - are attenuated differently, and
  - travel at different speeds through guided media
  
- This may lead to **delay distortion**

## Channel Capacity

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- Data rate
  - In bits per second, bps (not Bps)
  - Rate at which data can be communicated
- Bandwidth
  - In cycles per second, Hertz, Hz
  - Constrained by transmitter and medium
- Convention: not all "k"s are equal
  - data rates are given as power of 10
    - e.g., kHz is 1000Hz
  - data is given in terms of power of 2
    - e.g., KByte is 1024 Bytes

## **Nyquist Bandwidth**

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- If rate of signal transmission is  $2B$  then a signal with frequencies no greater than  $B$  is sufficient to carry the signal rate.
  - Why? Assume we have a square wave of repeating 101010. If a positive pulse is a 1 and a negative pulse is 0, then each pulse lasts  $1/2 T_1$  ( $T_1 = 1/f_1$ ) and the data rate is  $2f_1$  bits per second.

## **Nyquist Bandwidth**

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- If we limit the components to a maximum frequency (restrict the bandwidth) we need to make sure the signal is accurately represented.
- Based on the accuracy we require, the bandwidth can carry a particular data rate. The theoretical maximum communication limit is given by the **Nyquist** formula:

$$C = 2B \log_2 M$$

$C$  = capacity or data transfer rate in bps

$B$  = bandwidth (in hertz)

$M$  = number of possible signaling levels

## Signal Strength

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- An important parameter in communication is the strength of the signal transmitted. Even more important is the strength being received.
- As signal propagates it will be *attenuated* (decreased)
- Amplifiers* are inserted to increase signal strength
- Gains, losses and relative levels of signals are expressed in decibels
  - This is a logarithmic scale, but strength usually falls logarithmically
  - Calculation of gains and losses involves simple addition and subtraction
- Decibel measure of difference in two power levels is

$$N_{dB} = 10 \log_{10} \frac{P_1}{P_2}$$

## Physical Aspects

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- Signal Attenuation and Distortion
  - As a signal propagates across a transmission medium its amplitude decreases. This is known as **signal attenuation**.
  - A typical signal consists of a composition of many frequency components (Fourier Analysis). Due to the limited transmission bandwidth of a medium, the higher frequency components may not be able to be transmitted.
    - Recall the **Nyquist** formula

$$C = 2B \log_2 M \qquad \log_2(x) = \frac{\ln(x)}{\ln(2)}$$

## Shannon capacity

- A transmission line may experience interference from a number of sources, called **noise**. Noise is measured in terms of signal to noise power ratio, expressed in decibels:

$$\left(\frac{S}{N}\right)_{dB} = 10 \log_{10} \left(\frac{S}{N}\right)$$

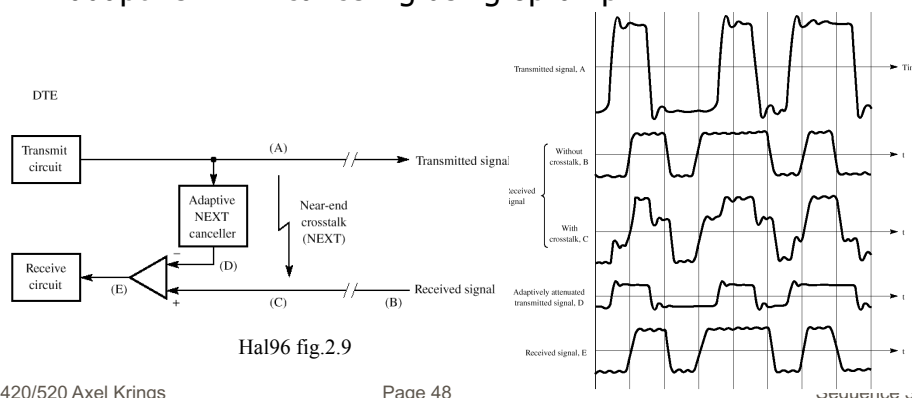
- The effects of noise on channel capacity can be seen using the **Shannon-Hartley Law**:

$$C = B \log_2 \left(1 + \frac{S}{N}\right) \text{ bps}$$

$C$  = data transfer rate in bps  
 $B$  = bandwidth (in Hertz)

## Cross Talk -- NEXT canceling

- near-end crosstalk (NEXT), cross talk of strong transmit (output) signal to weak receive (input) signal.
- adaptive NEXT canceling using op-amp





## Noise

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- Impulse Noise
  - impulse caused by switching, lightning etc.
- Thermal Noise
  - present irrespective of any external effects
  - caused by thermal agitation of electrons

## Noise

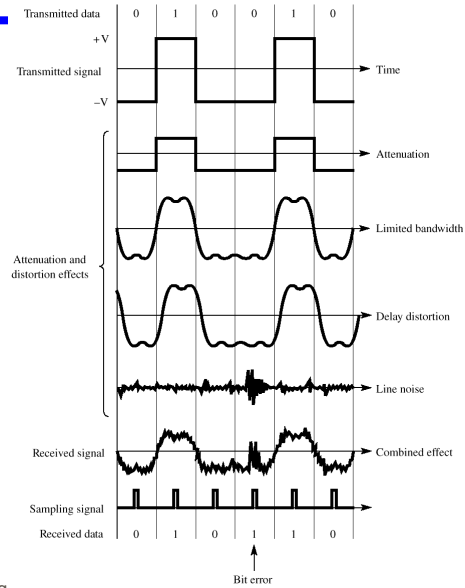
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- White Noise
  - random noise – entire spectrum
- Pink Noise
  - “realistic spectrum”
  - the power spectral density is inversely proportional to the frequency

## Combined Effects

- Attenuation
- Limited Bandwidth
- Noise

It all adds up!



Hal96 fig.2.6

## Thermal Noise

—Energy (in joules = watts x seconds) per bit in a signal:

$$E_b = ST_b$$

$S$  = signal power in watts  
 $T_b$  = time period for 1 bit in seconds

—Data Transmission rate  $R = 1/T_b$

—Thermal noise  $N_0$  in a line is: ( $T$  is temperature in K)

$$N_0 = kTW \text{ where } k = 1.3803 \times 10^{-23} \text{ joule K}^{-1}$$

$k$  is Boltzmann constant

$W$  is the bandwidth

$$\frac{E_b}{N_0} = \frac{S/R}{N_0} = \frac{S/R}{kTW}$$

## Signal Delay

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- There exists a **transmission propagation delay** in any medium
  - Speed of light  $3 \times 10^8 \text{ ms}^{-1}$
  - Speed of EM in cable/wire  $2 \times 10^8 \text{ ms}^{-1}$
- Important parameter is **round-trip-delay** (time from first bit sent to last bit acknowledged)

## Signal Delay

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- Propagation delay  $T_p$  and transmission delay  $T_x$

$$T_P = \frac{d}{V}, \quad T_x = \frac{n}{R}$$

- Important ratio  $\frac{T_P}{T_x}$

$d$  = distance in meters  
 $V$  = EM speed

$n$  = number of bits transmitted  
 $R$  = link bit rate in bits per second