Mathematical Analysis

• Let's continue Recursive Algorithms

Fibonacci numbers

The Fibonacci numbers:

0, 1, 1, 2, 3, 5, 8, 13, 21, ...

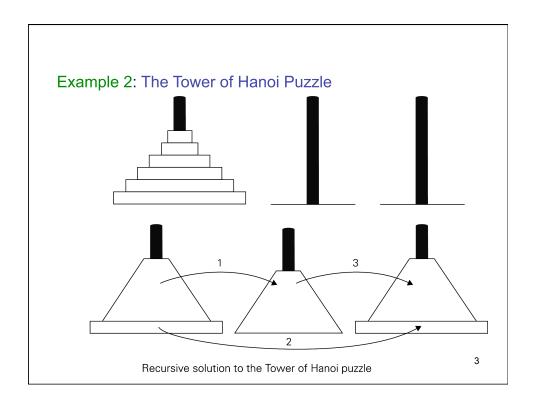
The Fibonacci recurrence:

F(n) = F(n-1) + F(n-2) F(0) = 0F(1) = 1

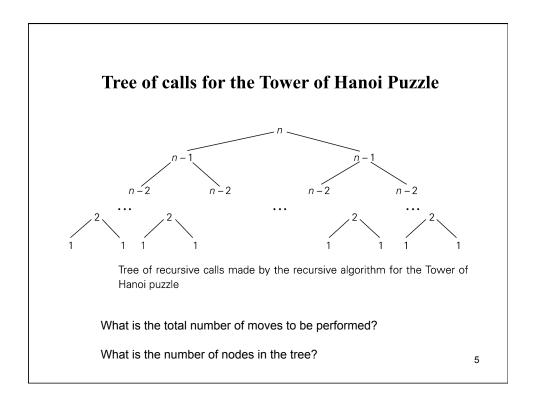
General 2nd order linear homogeneous recurrence with constant coefficients:

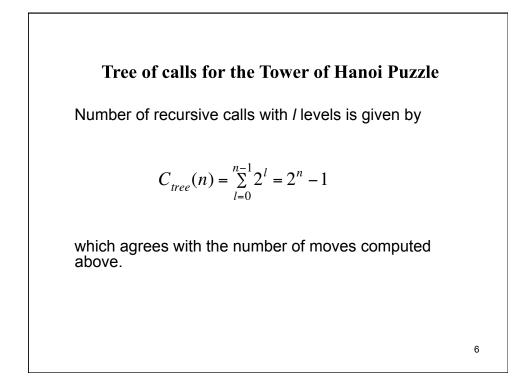
aX(n) + bX(n-1) + cX(n-2) = 0

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Example 2: The Tower of Hanoi PuzzleMumber of moves M(n) depends upon the number of
disks n only. The recurrence is given by $\mu(n) = \mu(n-1) + 1 + M(n-1) + n = n$ Mumber of M(n) = 1, thus the
securrence relation is given by M(1) = 1, thus the
 $\mu(1) = 1$ Mumber of M(n) = 2M(n-1) + 1 + for n > 1Moves other recurrence relation





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